

Full-Length Practice Test 5

Instructions: This practice test contains 280 multiple-choice questions divided into four parts. Select the best answer for each question.

Survey Of Natural Sciences

BIOLOGY (Questions 1–40)

1. Which cellular structure contains digestive enzymes that break down cellular waste and foreign materials?
 - A. Ribosome
 - B. Peroxisome
 - C. Lysosome
 - D. Golgi apparatus
2. The sinoatrial (SA) node is located in which chamber of the heart?
 - A. Left ventricle
 - B. Right atrium
 - C. Left atrium
 - D. Right ventricle
3. During which phase of the cell cycle does DNA replication occur?
 - A. G1 phase
 - B. G2 phase
 - C. M phase
 - D. S phase
4. The primary photosynthetic pigment in plants is:
 - A. Chlorophyll a
 - B. Chlorophyll b
 - C. Carotene
 - D. Xanthophyll
5. Which type of mutation involves the addition or deletion of nucleotides that shifts the reading frame?
 - A. Silent mutation
 - B. Missense mutation
 - C. Nonsense mutation

- D. Frameshift mutation
6. The gallbladder stores bile produced by which organ?
- A. Liver
 - B. Pancreas
 - C. Stomach
 - D. Spleen
7. In photosynthesis, NADPH is produced during:
- A. The Calvin cycle
 - B. Carbon fixation
 - C. Light-dependent reactions
 - D. Glycolysis
8. Okazaki fragments are formed during synthesis of which DNA strand?
- A. Lagging strand
 - B. Leading strand
 - C. Template strand
 - D. Coding strand
9. The hormone glucagon is secreted by which pancreatic cells?
- A. Beta cells
 - B. Delta cells
 - C. Acinar cells
 - D. Alpha cells
10. Which component of blood is primarily responsible for maintaining osmotic pressure?
- A. Red blood cells
 - B. White blood cells
 - C. Albumin
 - D. Fibrinogen
11. The vasa recta is associated with which kidney structure?
- A. Glomerulus
 - B. Loop of Henle
 - C. Distal tubule
 - D. Bowman's capsule
12. In eukaryotic cells, which RNA polymerase transcribes mRNA?
- A. RNA polymerase II

- B. RNA polymerase I
- C. RNA polymerase III
- D. DNA polymerase

13. Which blood vessels have valves to prevent backflow?

- A. Arteries
- B. Arterioles
- C. Capillaries
- D. Veins

14. The sodium-potassium pump transports:

- A. 2 Na⁺ out, 3 K⁺ in
- B. 2 K⁺ out, 3 Na⁺ in
- C. 3 Na⁺ out, 2 K⁺ in
- D. 3 K⁺ out, 2 Na⁺ in

15. Which nitrogenous waste product is the least toxic but requires the most water for excretion?

- A. Uric acid
- B. Urea
- C. Ammonia
- D. Creatinine

16. The lac operon in bacteria is an example of:

- A. Positive gene regulation
- B. Post-transcriptional regulation
- C. Post-translational regulation
- D. Negative gene regulation

17. Surfactant in the lungs functions to:

- A. Increase surface tension
- B. Facilitate gas exchange
- C. Prevent alveolar collapse
- D. Increase oxygen solubility

18. Which process produces four non-identical haploid cells?

- A. Mitosis
- B. Binary fission
- C. Meiosis
- D. Budding

19. The corpus luteum secretes primarily:
- A. Estrogen only
 - B. Progesterone
 - C. FSH
 - D. LH
20. Antibody diversity is generated primarily through:
- A. V(D)J recombination
 - B. Alternative splicing
 - C. Point mutations
 - D. Gene duplication
21. Which structure in plant cells is responsible for turgor pressure?
- A. Cell wall
 - B. Chloroplast
 - C. Nucleus
 - D. Central vacuole
22. The neurotransmitter acetylcholine is degraded by which enzyme?
- A. Monoamine oxidase
 - B. Catechol-O-methyltransferase
 - C. Acetylcholinesterase
 - D. Peptidase
23. In muscle contraction, calcium ions bind to:
- A. Actin
 - B. Troponin
 - C. Myosin
 - D. Tropomyosin
24. Which hormone stimulates ovulation?
- A. FSH
 - B. Estrogen
 - C. LH
 - D. Progesterone
25. The electron transport chain in cellular respiration is located in the:
- A. Cytoplasm
 - B. Inner mitochondrial membrane
 - C. Outer mitochondrial membrane

D. Mitochondrial matrix

26. Which immune cells are responsible for antibody production?

A. T lymphocytes

B. Plasma cells

C. Macrophages

D. Natural killer cells

27. The node of Ranvier is found in:

A. Myelinated axons

B. Dendrites

C. Cell bodies

D. Synapses

28. Cyclin-dependent kinases (CDKs) regulate:

A. DNA replication only

B. Transcription

C. Translation

D. Cell cycle progression

29. The trachea divides into two bronchi at the:

A. Larynx

B. Pharynx

C. Carina

D. Epiglottis

30. Which molecule directly provides energy for muscle contraction?

A. Glucose

B. ATP

C. ADP

D. Creatine phosphate

31. The semiconservative model of DNA replication was demonstrated by:

A. Watson and Crick

B. Franklin

C. Chargaff

D. Meselson and Stahl

32. In the menstrual cycle, the proliferative phase is stimulated by:

A. Estrogen

- B. Progesterone
- C. FSH
- D. LH

33. The majority of nutrient absorption occurs in the:

- A. Stomach
- B. Duodenum
- C. Jejunum and ileum
- D. Large intestine

34. Alternative splicing occurs during:

- A. DNA replication
- B. RNA processing
- C. Translation
- D. Transcription initiation

35. The blind spot in the eye is located where:

- A. Optic nerve exits the retina
- B. Lens attaches
- C. Cornea meets sclera
- D. Fovea centralis is located

36. Which enzyme breaks the hydrogen bonds between DNA base pairs during replication?

- A. Ligase
- B. Primase
- C. DNA polymerase
- D. Helicase

37. Red bone marrow is primarily responsible for:

- A. Fat storage
- B. Mineral storage
- C. Blood cell production
- D. Antibody storage

38. The Z-line (Z-disc) is a component of:

- A. Smooth muscle
- B. Sarcomeres
- C. Cardiac intercalated discs
- D. Tendons

39. Antidiuretic hormone (ADH) increases water reabsorption in the:
- A. Proximal tubule
 - B. Loop of Henle
 - C. Glomerulus
 - D. Collecting duct
40. In Hardy-Weinberg equilibrium, if the frequency of allele A is 0.7, the frequency of heterozygotes is:
- A. 0.42
 - B. 0.49
 - C. 0.21
 - D. 0.09

GENERAL CHEMISTRY (Questions 41-70)

41. What is the electron configuration of chlorine (atomic number 17)?
- A. $1s^2 2s^2 2p^6 3s^2 3p^4$
 - B. $1s^2 2s^2 2p^6 3s^2 3p^6$
 - C. $1s^2 2s^2 2p^6 3s^2 3p^5$
 - D. $1s^2 2s^2 2p^6 3s^1 3p^6$
42. According to the Aufbau principle, electrons fill orbitals:
- A. Randomly
 - B. From lowest to highest energy
 - C. From highest to lowest energy
 - D. Only in the valence shell
43. The pH of a 0.001 M HCl solution is:
- A. 3
 - B. 11
 - C. -3
 - D. 7
44. Which of the following exhibits the highest boiling point?
- A. CH_4
 - B. NH_3
 - C. H_2O
 - D. HF
45. In the reaction $2\text{H}_2 + \text{O}_2 \rightarrow 2\text{H}_2\text{O}$, oxygen is:

- A. Oxidized
- B. Reduced
- C. Neither oxidized nor reduced
- D. Both oxidized and reduced

46. The maximum number of electrons in the $n=3$ energy level is:

- A. 2
- B. 8
- C. 18
- D. 32

47. Which quantum number describes the orientation of an orbital in space?

- A. Principal (n)
- B. Angular momentum (l)
- C. Spin (s)
- D. Magnetic (m)

48. A buffer solution is most effective when pH equals:

- A. pK_a
- B. 7
- C. 14
- D. $pK_a + 1$

49. The ideal gas law is represented by:

- A. $P_1V_1 = P_2V_2$
- B. $PV = nRT$
- C. $V_1/T_1 = V_2/T_2$
- D. $P_1/T_1 = P_2/T_2$

50. What is the oxidation state of nitrogen in HNO_3 ?

- A. +3
- B. +4
- C. +5
- D. +6

51. Hess's Law states that enthalpy change is:

- A. Path independent
- B. Path dependent
- C. Always positive
- D. Always negative

52. How many grams are in 2.5 moles of NaCl (molar mass = 58.5 g/mol)?
- A. 23.4 g
 - B. 58.5 g
 - C. 117 g
 - D. 146.25 g
53. Which has the smallest atomic radius?
- A. Na
 - B. F
 - C. Cl
 - D. K
54. The common ion effect describes:
- A. Increased solubility with added ions
 - B. Neutral pH in salt solutions
 - C. Decreased solubility with common ions
 - D. Increased reaction rate
55. In the equation $\Delta G = \Delta H - T\Delta S$, a spontaneous reaction has ΔG :
- A. < 0
 - B. $= 0$
 - C. > 0
 - D. $= \Delta H$
56. The concentration of a solution containing 4 moles of solute in 2 liters is:
- A. 0.5 M
 - B. 2 M
 - C. 6 M
 - D. 2 M
57. Sigma bonds are formed by:
- A. Side-by-side orbital overlap
 - B. Pi orbital overlap
 - C. End-to-end orbital overlap
 - D. No orbital overlap
58. A weak acid has a:
- A. High K_a
 - B. Low K_a

- C. High pH
- D. $K_a = 1$

59. The half-life of a radioactive substance is 20 years. What fraction remains after 60 years?

- A. $1/2$
- B. $1/4$
- C. $1/6$
- D. $1/8$

60. Which element is most electronegative?

- A. Fluorine
- B. Oxygen
- C. Nitrogen
- D. Chlorine

61. The molecular geometry of ammonia (NH_3) is:

- A. Tetrahedral
- B. Bent
- C. Trigonal pyramidal
- D. Trigonal planar

62. In a galvanic cell, reduction occurs at the:

- A. Anode
- B. Cathode
- C. Salt bridge
- D. Neither electrode

63. The units of the gas constant R are:

- A. J/mol
- B. L/mol
- C. $\text{atm}\cdot\text{L}/\text{mol}$
- D. $\text{atm}\cdot\text{L}/(\text{mol}\cdot\text{K})$

64. Isotopes differ in the number of:

- A. Neutrons
- B. Protons
- C. Electrons
- D. Orbitals

65. The rate law for a zero-order reaction is:

- A. Rate = $k[A]$
- B. Rate = $k[A]^2$
- C. Rate = k
- D. Rate = $k/[A]$

66. The conjugate base of H_2SO_4 is:

- A. HSO_4^-
- B. SO_4^{2-}
- C. $H_3SO_4^+$
- D. HSO_4^-

67. Resonance structures differ in the placement of:

- A. Electrons
- B. Atoms
- C. Protons
- D. Neutrons

68. At constant temperature, doubling the volume of a gas:

- A. Doubles the pressure
- B. Quadruples the pressure
- C. Has no effect on pressure
- D. Halves the pressure

69. The oxidation number of an element in its standard state is:

- A. +1
- B. 0
- C. -1
- D. Variable

70. Which colligative property is used in automotive antifreeze?

- A. Osmotic pressure
- B. Vapor pressure lowering
- C. Freezing point depression
- D. Boiling point elevation

ORGANIC CHEMISTRY (Questions 71-100)

71. The general formula for alkenes is:
- A. C_nH_{2n+2}
 - B. C_nH_{2n}
 - C. C_nH_n
 - D. C_nH_{2n}
72. Which functional group is present in aldehydes?
- A. -CHO
 - B. -COOH
 - C. -CO- (between carbons)
 - D. -OH
73. The IUPAC name for CH_3CH_2OH is:
- A. Methanol
 - B. Propanol
 - C. Ethanol
 - D. Butanol
74. Geometric isomers (cis-trans) are possible when:
- A. There is free rotation around a bond
 - B. A double bond has different groups attached
 - C. There are four different groups on a carbon
 - D. There is a triple bond
75. Which reaction adds water across a double bond?
- A. Hydration
 - B. Hydrogenation
 - C. Halogenation
 - D. Dehydration
76. The most reactive carbonyl compound toward nucleophilic addition is:
- A. Ester
 - B. Acid chloride
 - C. Amide
 - D. Carboxylic acid
77. Which reagent distinguishes primary, secondary, and tertiary alcohols?
- A. $NaBH_4$
 - B. $LiAlH_4$

- C. Lucas reagent
- D. Tollens' reagent

78. The hybridization of carbon in acetylene (C_2H_2) is:

- A. sp
- B. sp^2
- C. sp^3
- D. sp^3d

79. Anti-Markovnikov addition is achieved using:

- A. H_2SO_4/H_2O
- B. HBr
- C. HCl
- D. Hydroboration-oxidation

80. Which compound is aromatic?

- A. Cyclohexene
- B. Benzene
- C. Cyclopentane
- D. 1,3-cyclohexadiene

81. The S_N2 mechanism proceeds via:

- A. Backside attack
- B. Carbocation formation
- C. Radical intermediate
- D. Frontside attack

82. Carboxylic acids are more acidic than alcohols because:

- A. They have more oxygen atoms
- B. They are larger molecules
- C. The conjugate acid is more stable
- D. The conjugate base is stabilized by resonance

83. The Wittig reaction forms:

- A. Alcohols
- B. Aldehydes
- C. Alkenes
- D. Ketones

84. In $E1$ reactions, the rate-determining step is:

- A. Proton removal
- B. Carbocation formation
- C. Nucleophilic attack
- D. Double bond formation

85. Which is the strongest base?

- A. CH_3COO^-
- B. Cl^-
- C. OH^-
- D. NH_2^-

86. Esterification is the reaction between:

- A. Carboxylic acid and alcohol
- B. Aldehyde and alcohol
- C. Ketone and alcohol
- D. Alcohol and alkene

87. A chiral carbon must have:

- A. Four different groups attached
- B. A double bond
- C. At least one hydrogen
- D. A functional group

88. The Friedel-Crafts alkylation uses:

- A. NaBH_4
- B. H_2/Pd
- C. AlCl_3 catalyst
- D. KMnO_4

89. Which undergoes nucleophilic substitution most readily?

- A. CH_3F
- B. CH_3Cl
- C. CH_3Br
- D. CH_3I

90. The aldol condensation involves:

- A. Alkene and aldehyde
- B. Two aldehydes or ketones
- C. Alcohol and acid
- D. Ester and alcohol

91. In the Cahn-Ingold-Prelog priority rules, priority is based on:
- A. Alphabetical order
 - B. Size
 - C. Electronegativity
 - D. Atomic number
92. Primary amines can be prepared by:
- A. Gabriel synthesis
 - B. Friedel-Crafts acylation
 - C. Aldol condensation
 - D. Claisen condensation
93. Enantiomers have:
- A. Different molecular formulas
 - B. Different connectivities
 - C. Opposite optical rotations
 - D. Identical physical properties including optical rotation
94. The Clemmensen reduction reduces:
- A. Alkenes to alkanes
 - B. Ketones to alkanes
 - C. Alcohols to alkanes
 - D. Alkynes to alkenes
95. Tertiary alcohols cannot be oxidized because:
- A. They lack a hydrogen on the carbon bearing OH
 - B. They are too stable
 - C. They are too large
 - D. The oxygen is shielded
96. Electrophilic aromatic substitution on toluene favors:
- A. Meta position
 - B. Para position only
 - C. Ortho and para positions
 - D. No substitution occurs
97. The Hofmann elimination produces:
- A. The more substituted alkene
 - B. The less substituted alkene

- C. No alkene
- D. Only cyclic products

98. Saponification is:

- A. Base-catalyzed ester hydrolysis
- B. Acid-catalyzed ester hydrolysis
- C. Ester formation
- D. Aldehyde reduction

99. Mass spectrometry determines:

- A. Functional groups
- B. Carbon skeleton
- C. Boiling point
- D. Molecular weight

100. In ^1H NMR, the integration indicates:

- A. Chemical shift
- B. Number of equivalent hydrogens
- C. Splitting pattern
- D. Peak width

Perceptual Ability Test

ANGLE DISCRIMINATION (Questions 1-15)

Directions: Four angles are described. Rank them from SMALLEST to LARGEST.

1. [Angle Ranking] Four angles: Angle 1 = 54° , Angle 2 = 47° , Angle 3 = 38° , Angle 4 = 62° . Rank from smallest to largest.
 - A. 2-3-1-4
 - B. 3-1-2-4
 - C. 3-2-1-4
 - D. 1-2-3-4

2. [Angle Ranking] Angle P = 69° , Angle Q = 58° , Angle R = 75° , Angle S = 52° . Rank from smallest to largest.
 - A. S-P-Q-R
 - B. S-Q-P-R
 - C. Q-S-P-R
 - D. S-R-Q-P

3. [Angle Ranking] Four angles measure: Angle 1 = 24° , Angle 2 = 36° , Angle 3 = 42° , Angle 4 = 50° . Rank from smallest to largest.
- A. 1-2-3-4
 - B. 1-3-2-4
 - C. 2-1-3-4
 - D. 4-3-2-1
4. [Angle Ranking] Angle A = 81° , Angle B = 74° , Angle C = 87° , Angle D = 79° . Rank from smallest to largest.
- A. A-B-C-D
 - B. B-A-C-D
 - C. B-C-D-A
 - D. B-D-A-C
5. [Angle Ranking] Angle W is two-thirds of a right angle. Angle X = 48° . Angle Y = 56° . Angle Z = 72° . Rank from smallest to largest.
- A. W-Y-X-Z
 - B. X-Y-W-Z
 - C. X-W-Y-Z
 - D. W-X-Z-Y
6. [Angle Ranking] Four angles: Angle 1 = 15° , Angle 2 = 29° , Angle 3 = 36° , Angle 4 = 43° . Rank from smallest to largest.
- A. 1-2-3-4
 - B. 1-3-2-4
 - C. 2-1-3-4
 - D. 4-3-2-1
7. [Angle Ranking] Angle M = 61° , Angle N = 73° , Angle O = 55° , Angle P = 68° . Rank from smallest to largest.
- A. M-O-P-N
 - B. O-M-P-N
 - C. O-P-M-N
 - D. M-P-O-N
8. [Angle Ranking] Four angles measure: Angle 1 = 20° , Angle 2 = 32° , Angle 3 = 27° , Angle 4 = 39° . Rank from smallest to largest.
- A. 1-2-3-4
 - B. 1-4-3-2
 - C. 2-1-3-4

D. 1-3-2-4

9. [Angle Ranking] Angle A = 46° , Angle B = 52° , Angle C = 35° , Angle D = 64° . Rank from smallest to largest.
- A. C-A-B-D
 - B. C-B-A-D
 - C. A-C-B-D
 - D. C-A-D-B
10. [Angle Ranking] Four angles: Angle 1 = 70° , Angle 2 = 63° , Angle 3 = 77° , Angle 4 = 66° . Rank from smallest to largest.
- A. 2-1-4-3
 - B. 2-4-1-3
 - C. 2-4-1-3
 - D. 4-2-1-3
11. [Angle Ranking] Angle W = 33° , Angle X = 51° , Angle Y = 45° , Angle Z = 40° . Rank from smallest to largest.
- A. W-Y-Z-X
 - B. W-Z-Y-X
 - C. Z-W-Y-X
 - D. W-X-Y-Z
12. [Angle Ranking] Four angles measure: Angle 1 = 17° , Angle 2 = 25° , Angle 3 = 31° , Angle 4 = 44° . Rank from smallest to largest.
- A. 1-3-2-4
 - B. 1-2-3-4
 - C. 2-1-3-4
 - D. 1-2-4-3
13. [Angle Ranking] Angle P = 67° , Angle Q = 49° , Angle R = 78° , Angle S = 54° . Rank from smallest to largest.
- A. Q-S-P-R
 - B. S-P-Q-R
 - C. Q-S-P-R
 - D. S-Q-R-P
14. [Angle Ranking] Four angles: Angle 1 = 26° , Angle 2 = 40° , Angle 3 = 34° , Angle 4 = 48° . Rank from smallest to largest.
- A. 1-3-2-4

- B. 1-2-3-4
- C. 3-1-2-4
- D. 2-1-3-4

15. [Angle Ranking] Angle A = 76° , Angle B = 84° , Angle C = 89° , Angle D = 71° . Rank from smallest to largest.
- A. A-B-D-C
 - B. D-B-A-C
 - C. D-A-C-B
 - D. D-A-B-C

PAPER FOLDING (Questions 16-30)

Directions: A square piece of paper is folded one or more times, then hole(s) are punched. Determine the result when unfolded.

16. [Hole Punching] Paper is folded in half once, then three holes are punched through both layers. How many total holes appear when unfolded?
- A. 3
 - B. 6
 - C. 8
 - D. 4
17. [Hole Punching] Paper is folded three times (creating 8 layers), then two holes are punched through all layers. How many total holes appear when unfolded?
- A. 8
 - B. 12
 - C. 16
 - D. 24
18. [Hole Punching] Paper is folded in half once, then one hole is punched exactly on the fold line. How many holes appear when unfolded?
- A. 1
 - B. 2
 - C. 3
 - D. 4
19. [Hole Punching] Paper is folded in half once diagonally, then one hole is punched on the fold line. How many holes appear when unfolded?
- A. 1

- B. 2
- C. 4
- D. 3

20. [Hole Punching] Paper is folded in half once, then one hole is punched near the edge away from the fold. How many holes appear when unfolded?

- A. 1
- B. 2
- C. 4
- D. 8

21. [Hole Punching] Paper is folded three times, then one hole is punched through all layers. How many holes appear when unfolded?

- A. 4
- B. 6
- C. 16
- D. 8

22. [Hole Punching] Paper is folded in half twice (creating 4 layers), then one hole is punched through all layers. How many holes appear when unfolded?

- A. 4
- B. 2
- C. 8
- D. 6

23. [Hole Punching] Paper is folded in half once, then two holes are punched through both layers. How many total holes appear when unfolded?

- A. 2
- B. 6
- C. 4
- D. 8

24. [Hole Punching] Paper is folded in half twice, then a hole is punched at the point where both folds meet (center). How many holes appear when unfolded?

- A. 1
- B. 2
- C. 8
- D. 4

25. [Hole Punching] Paper is folded in half once vertically, then three holes are punched through both layers. How many total holes appear when unfolded?
- A. 3
 - B. 6
 - C. 4
 - D. 8
26. [Hole Punching] Paper is folded diagonally once, then two holes are punched away from the fold. How many total holes appear when unfolded?
- A. 4
 - B. 2
 - C. 6
 - D. 8
27. [Hole Punching] Paper is folded in half twice (into quarters), then one hole is punched at an edge (not corner). How many holes appear when unfolded?
- A. 2
 - B. 8
 - C. 4
 - D. 6
28. [Hole Punching] Paper is folded in half twice, then two holes are punched through all layers. How many total holes appear when unfolded?
- A. 4
 - B. 6
 - C. 16
 - D. 8
29. [Hole Punching] Paper is folded in half once, then four holes are punched through both layers. How many total holes appear when unfolded?
- A. 4
 - B. 8
 - C. 6
 - D. 12
30. [Hole Punching] Paper is folded in half twice, then one hole is punched in a corner of the folded paper. How many holes appear when unfolded?
- A. 2
 - B. 8
 - C. 4

D. 1

CUBE COUNTING (Questions 31-45)

Directions: Answer questions about unit cubes in various structures.

31. [Cube Counting] In a $3 \times 3 \times 3$ cube, how many unit cubes have exactly 0 faces exposed (completely interior)?
- A. 1
 - B. 4
 - C. 27
 - D. 8
32. [Cube Counting] A solid $4 \times 4 \times 4$ cube. How many unit cubes have exactly 3 faces exposed (corner cubes)?
- A. 4
 - B. 6
 - C. 12
 - D. 8
33. [Cube Counting] A $2 \times 3 \times 5$ rectangular prism. How many total unit cubes are in the structure?
- A. 10
 - B. 30
 - C. 18
 - D. 24
34. [Cube Counting] A structure of 8 unit cubes arranged in a straight line. How many cubes have exactly 5 faces exposed (end cubes)?
- A. 2
 - B. 0
 - C. 4
 - D. 1
35. [Cube Counting] In a $6 \times 6 \times 6$ cube, how many unit cubes have exactly 0 faces exposed?
- A. 8
 - B. 27
 - C. 64
 - D. 125

36. [Cube Counting] A $3 \times 4 \times 3$ rectangular prism. How many unit cubes have exactly 3 faces exposed (corners)?
- A. 6
 - B. 12
 - C. 4
 - D. 8
37. [Cube Counting] A solid $3 \times 3 \times 3$ cube. How many unit cubes have exactly 2 faces exposed (edge cubes)?
- A. 8
 - B. 12
 - C. 24
 - D. 6
38. [Cube Counting] A $2 \times 2 \times 6$ rectangular prism. How many total unit cubes are in the structure?
- A. 10
 - B. 20
 - C. 24
 - D. 16
39. [Cube Counting] In a $5 \times 5 \times 5$ cube, how many unit cubes have exactly 1 face exposed (face cubes)?
- A. 54
 - B. 48
 - C. 32
 - D. 24
40. [Cube Counting] A $4 \times 3 \times 3$ rectangular prism. How many unit cubes are NOT corner cubes?
- A. 28
 - B. 30
 - C. 32
 - D. 28
41. [Cube Counting] A pyramid structure: 9 cubes on bottom (3×3), 4 cubes on middle layer (2×2), 1 cube on top (14 total). How many cubes have exactly 3 exposed faces?
- A. 4
 - B. 5
 - C. 1
 - D. 2

42. [Cube Counting] A $3 \times 3 \times 5$ rectangular prism. How many unit cubes have exactly 2 faces exposed?
- A. 22
 - B. 18
 - C. 20
 - D. 24
43. [Cube Counting] An L-shaped structure: 6 cubes in a row with 2 cubes stacked on one end (8 total). How many cubes have exactly 3 exposed faces?
- A. 2
 - B. 4
 - C. 3
 - D. 5
44. [Cube Counting] A $5 \times 5 \times 2$ rectangular prism. How many unit cubes have at least one face exposed?
- A. 48
 - B. 45
 - C. 40
 - D. 50
45. [Cube Counting] In a $2 \times 2 \times 2$ cube, how many unit cubes have exactly 2 faces exposed?
- A. 8
 - B. 0
 - C. 6
 - D. 4

PATTERN FOLDING (Questions 46-60)

Directions: Identify what 3D shape is formed when the described net is folded.

46. [Pattern Folding] A net consists of 5 squares in a plus/cross shape (one center, four extending from each edge). What does it form?
- A. Complete cube
 - B. Pyramid
 - C. Open-top cube
 - D. Prism

47. [Pattern Folding] A net has 1 square with 4 triangles attached to each edge of the square. What 3D shape is formed?
- A. Square pyramid
 - B. Cube
 - C. Tetrahedron
 - D. Triangular prism
48. [Pattern Folding] A net shows 2 triangles and 3 rectangles all connected. What shape does it form?
- A. Tetrahedron
 - B. Square pyramid
 - C. Cube
 - D. Triangular prism
49. [Pattern Folding] A net consists of 4 equilateral triangles in a connected arrangement. What shape does it form?
- A. Square pyramid
 - B. Tetrahedron
 - C. Octahedron
 - D. Cube
50. [Pattern Folding] A net shows 1 pentagon with 5 triangles attached to each edge. What 3D shape is formed?
- A. Pentagonal pyramid
 - B. Cube
 - C. Hexagonal pyramid
 - D. Triangular prism
51. [Pattern Folding] A net consists of 6 squares arranged in a T-shape (4 in a row, 1 above and 1 below the second square). What does it form?
- A. Pyramid
 - B. Cube
 - C. Open box
 - D. Prism
52. [Pattern Folding] A net shows 1 hexagon with 6 rectangles attached to its edges. What 3D shape does it form?
- A. Cube
 - B. Hexagonal pyramid
 - C. Hexagonal prism

D. Rectangular prism

53. [Pattern Folding] A net consists of 4 squares in an L-shape. What does it form when folded?

- A. Partial cube (open box)
- B. Complete cube
- C. Pyramid
- D. Prism

54. [Pattern Folding] A net shows 6 rectangles arranged to form a closed shape. What is it most likely to form?

- A. Cube
- B. Pyramid
- C. Triangular prism
- D. Rectangular prism

55. [Pattern Folding] A net consists of 1 square and 3 triangles attached to three edges of the square. What partial shape does it form?

- A. Partial pyramid (missing one face)
- B. Complete pyramid
- C. Cube
- D. Prism

56. [Pattern Folding] A net shows 2 hexagons with 6 rectangles connecting them. What 3D shape is formed?

- A. Rectangular prism
- B. Hexagonal pyramid
- C. Cube
- D. Hexagonal prism

57. [Pattern Folding] A net consists of 1 large triangle with 3 smaller triangles attached to its edges. What shape does it form?

- A. Octahedron
- B. Square pyramid
- C. Tetrahedron
- D. Triangular prism

58. [Pattern Folding] A net shows 6 equal squares in a cross pattern. What does it form?

- A. Cube
- B. Pyramid
- C. Open box

D. Prism

59. [Pattern Folding] A net consists of irregular polygons that don't match standard shapes. What type of shape might this form?
- A. Regular pyramid
 - B. Irregular polyhedron
 - C. Cube
 - D. Standard prism
60. [Pattern Folding] A net shows 3 squares in a row with 1 square attached to the side of the middle square (T-shape). What can this form?
- A. Complete cube
 - B. Pyramid
 - C. Prism
 - D. Open-top cube

APERTURES / KEYHOLES (Questions 61-75)

Directions: Determine which aperture shape a 3D object could pass through.

61. [Keyhole] A rectangular prism passes through an aperture. Which shape is possible?
- A. Circle
 - B. Triangle
 - C. Rectangle
 - D. Pentagon
62. [Keyhole] A cone must pass through an aperture. Which aperture shape could work?
- A. Square
 - B. Circle or Triangle
 - C. Pentagon
 - D. Hexagon
63. [Keyhole] A cube is oriented to pass through an aperture. Which aperture shape is possible?
- A. Square
 - B. Triangle
 - C. Circle
 - D. Pentagon
64. [Keyhole] A sphere passes through an aperture. Which shape would work?

- A. Square
- B. Triangle
- C. Circle
- D. Rectangle

65. [Keyhole] A triangular prism passes through an aperture. Which shape could work?

- A. Circle
- B. Pentagon
- C. Hexagon
- D. Triangle or Rectangle

66. [Keyhole] Which aperture shape would NOT work for a cylinder?

- A. Triangle
- B. Circle
- C. Rectangle
- D. Oval

67. [Keyhole] A square pyramid must pass through an aperture. Which aperture is possible?

- A. Circle
- B. Pentagon
- C. Hexagon
- D. Square or Triangle

68. [Keyhole] A hexagonal prism passes through an aperture. Which shape is possible?

- A. Circle
- B. Hexagon or Rectangle
- C. Triangle
- D. Pentagon

69. [Keyhole] A tetrahedron (4-faced triangular pyramid) passes through an aperture. Which shape works?

- A. Triangle
- B. Square
- C. Pentagon
- D. Hexagon

70. [Keyhole] Which 3D object could pass through a circular aperture?

- A. Cube only
- B. Triangular prism only
- C. Sphere or Cylinder

D. Pyramid only

71. [Keyhole] An octahedron passes through an aperture. Which shape is most likely?
- A. Pentagon
 - B. Hexagon
 - C. Circle
 - D. Triangle or Square
72. [Keyhole] A pentagonal prism passes through an aperture. Which shape could work?
- A. Triangle
 - B. Pentagon or Rectangle
 - C. Circle
 - D. Hexagon
73. [Keyhole] Which aperture shape would work for a rectangular prism but NOT for a sphere?
- A. Circle
 - B. Oval
 - C. Rectangle
 - D. Triangle
74. [Keyhole] A cylinder passes through an aperture. Which is NOT a possible aperture shape?
- A. Triangle
 - B. Circle
 - C. Rectangle
 - D. Oval
75. [Keyhole] Which 3D shape could pass through both a triangular and rectangular aperture?
- A. Sphere
 - B. Cube
 - C. Cylinder
 - D. Triangular prism

VIEW RECOGNITION (Questions 76-90)

Directions: Given views from different angles, identify the 3D shape or determine what a view would look like.

76. [Top-Front-End] Top view: square. Front view: triangle. Side view: triangle. What is the shape?
- A. Cone
 - B. Square pyramid
 - C. Cylinder

D. Cube

77. [Top-Front-End] Front view: rectangle. Top view: circle. Side view: rectangle. What is the shape?
- A. Cylinder
 - B. Cone
 - C. Square pyramid
 - D. Rectangular prism
78. [Top-Front-End] All three views (top, front, side) show identical circles. What is the shape?
- A. Cylinder
 - B. Cone
 - C. Sphere
 - D. Cube
79. [Top-Front-End] A cube is viewed from the top. What shape appears?
- A. Circle
 - B. Rectangle
 - C. Triangle
 - D. Square
80. [Top-Front-End] Top view: triangle. Front view: rectangle. Side view: rectangle. What is the shape?
- A. Square pyramid
 - B. Triangular prism
 - C. Tetrahedron
 - D. Cone
81. [Top-Front-End] Top view: hexagon. Front and side views: rectangles. What is the shape?
- A. Cube
 - B. Hexagonal pyramid
 - C. Hexagonal prism
 - D. Rectangular prism
82. [Top-Front-End] A cylinder is viewed from the side (perpendicular to its axis). What shape appears?
- A. Circle
 - B. Square
 - C. Triangle
 - D. Rectangle

83. [Top-Front-End] All three views (top, front, side) show identical squares. What is the shape?
- A. Cube
 - B. Square pyramid
 - C. Cylinder
 - D. Rectangular prism
84. [Top-Front-End] Top view: pentagon. Front and side views: rectangles. What is the shape?
- A. Rectangular prism
 - B. Pentagonal pyramid
 - C. Pentagonal prism
 - D. Pentagon
85. [Top-Front-End] A triangular prism is viewed from the end (looking at the triangular face). What shape appears?
- A. Rectangle
 - B. Triangle
 - C. Circle
 - D. Square
86. [Top-Front-End] A cone is viewed from directly above (top view). What shape appears?
- A. Triangle
 - B. Circle
 - C. Rectangle
 - D. Square
87. [Top-Front-End] Top view: rectangle. Front view: rectangle. Side view: square. What is the shape?
- A. Cube
 - B. Cylinder
 - C. Rectangular prism
 - D. Pyramid
88. [Top-Front-End] A square pyramid is viewed from directly above. What shape appears?
- A. Triangle
 - B. Circle
 - C. Rectangle
 - D. Square

89. [Top-Front-End] Top view: circle. Front view: triangle. Side view: triangle. What is the 3D shape?
- A. Cylinder
 - B. Sphere
 - C. Square pyramid
 - D. Cone
90. [Top-Front-End] Top view: L-shape. Front view: rectangle. Side view: rectangle. What type of structure is this?
- A. L-shaped block structure
 - B. Pyramid
 - C. Cylinder
 - D. D. Cube

Reading Comprehension

PASSAGE I

The blood-brain barrier (BBB) represents one of the body's most selective biological interfaces, protecting the central nervous system from potentially harmful substances while allowing essential nutrients to pass. Unlike typical capillaries that permit relatively free exchange between blood and surrounding tissues, brain capillaries feature tight junctions between endothelial cells, creating an exceptionally restrictive barrier. This selectivity poses significant challenges for treating neurological diseases, as approximately 98% of small-molecule drugs and virtually all large-molecule therapeutics cannot cross the BBB.

The BBB's structure involves multiple components working together. Endothelial cells lining brain capillaries are connected by tight junction proteins that seal gaps between cells, preventing paracellular transport (movement between cells). These endothelial cells also lack fenestrations (pores) common in other capillaries and contain fewer pinocytotic vesicles, further limiting transcellular transport. Astrocyte end-feet wrap around capillaries, releasing signals that maintain barrier properties. Pericytes embedded in the capillary basement membrane provide structural support and regulate blood flow.

Selective transport across the BBB occurs through specific mechanisms. Glucose enters via GLUT1 transporters, essential amino acids use carrier-mediated transport, and lipid-soluble molecules can diffuse through endothelial cell membranes if sufficiently small and uncharged. The BBB also actively protects the brain through efflux transporters like P-glycoprotein that pump potentially harmful substances back into the bloodstream. This protective mechanism, while beneficial against toxins, also excludes many therapeutic drugs designed to treat brain diseases.

Certain brain regions called circumventricular organs lack a complete blood-brain barrier, allowing direct monitoring of blood composition. The area postrema, located in the brainstem, detects toxins in blood and triggers vomiting. The median eminence permits hormone exchange between blood and the hypothalamus. The subfornical organ and organum vasculosum respond to circulating signals regulating thirst and blood pressure. These specialized regions demonstrate that the BBB is strategically incomplete where sensing blood-borne signals provides survival advantages.

Diseases and injuries can compromise BBB integrity with serious consequences. Brain tumors often disrupt the barrier, allowing contrast agents used in MRI to leak into brain tissue, actually aiding diagnosis. Multiple sclerosis involves inflammatory breakdown of the BBB, permitting immune cell infiltration that damages myelin. Traumatic brain injury can cause both immediate barrier rupture and delayed dysfunction lasting weeks. Stroke creates regions where barrier breakdown allows brain edema (swelling) that worsens outcomes. Understanding BBB pathology has become crucial for developing neuroprotective strategies and improving drug delivery to the diseased brain.

1. According to the passage, approximately what percentage of small-molecule drugs cannot cross the BBB?
 - A. 50%
 - B. 98%
 - C. 75%
 - D. 100%
2. Tight junctions between endothelial cells prevent:
 - A. Paracellular transport
 - B. All transport
 - C. Glucose transport
 - D. Lipid diffusion
3. The passage indicates that brain capillary endothelial cells lack:
 - A. Tight junctions
 - B. Transporters
 - C. Astrocyte contact
 - D. Fenestrations
4. Astrocyte end-feet function to:
 - A. Transport glucose
 - B. Pump out toxins
 - C. Maintain barrier properties
 - D. Create tight junctions

5. GLUT1 transporters specifically allow passage of:
 - A. Amino acids
 - B. Glucose
 - C. Lipids
 - D. Proteins

6. P-glycoprotein functions as:
 - A. A glucose transporter
 - B. A tight junction protein
 - C. An amino acid carrier
 - D. An efflux pump

7. Circumventricular organs are characterized by:
 - A. Lacking a complete blood-brain barrier
 - B. Having the strongest barriers
 - C. Containing no blood vessels
 - D. Being located only in the cortex

8. The area postrema's function is to:
 - A. Regulate blood pressure
 - B. Control thirst
 - C. Detect blood toxins and trigger vomiting
 - D. Produce hormones

9. The median eminence permits exchange between blood and:
 - A. The cerebellum
 - B. The hypothalamus
 - C. The cortex
 - D. The brainstem

10. In brain tumor diagnosis, BBB disruption:
 - A. Aids diagnosis by allowing contrast agent leakage
 - B. Prevents all imaging
 - C. Has no diagnostic value
 - D. Only occurs in late stages

11. Multiple sclerosis involves BBB breakdown that permits:
 - A. Glucose entry
 - B. Oxygen transport
 - C. Nutrient absorption

D. Immune cell infiltration

12. According to the passage, traumatic brain injury can cause BBB dysfunction lasting:

A. Hours only

B. Days only

C. Weeks

D. Permanently always

13. Brain edema (swelling) after stroke results from:

A. Increased blood flow

B. Barrier breakdown

C. Neuron growth

D. Astrocyte expansion

14. The passage suggests that P-glycoprotein's protective function also:

A. Enhances all drug delivery

B. Has no effect on treatment

C. Increases nutrient transport

D. Excludes many therapeutic drugs

15. Lipid-soluble molecules can cross the BBB if they are:

A. Sufficiently small and uncharged

B. Large and charged

C. Proteins

D. Glucose-based

16. Pericytes embedded in capillary basement membrane provide:

A. Hormone production

B. Structural support and blood flow regulation

C. Neurotransmitter synthesis

D. Immune defense only

17. The subfornical organ responds to circulating signals regulating:

A. Digestion

B. Vision

C. Thirst and blood pressure

D. Hearing

PASSAGE II

Antibiotic resistance represents one of the most urgent global health threats, with bacteria evolving resistance mechanisms faster than new antibiotics are developed. The World Health Organization warns that without action, common infections could become untreatable, returning medicine to the pre-antibiotic era when minor injuries could prove fatal. Understanding how resistance emerges and spreads is essential for preserving antibiotic effectiveness for future generations.

Bacteria acquire resistance through multiple mechanisms. Genetic mutations can alter antibiotic target sites, preventing drug binding. For example, mutations in bacterial ribosomes can block tetracycline binding, rendering it ineffective. Bacteria also produce enzymes that destroy antibiotics—beta-lactamases break down penicillin and related drugs by cleaving their beta-lactam ring structure. Efflux pumps actively expel antibiotics from bacterial cells before they can act. Some bacteria modify their cell membranes to prevent antibiotic entry. These resistance mechanisms can arise spontaneously through mutation or be acquired from other bacteria through horizontal gene transfer.

Horizontal gene transfer accelerates resistance spread dramatically. Bacteria can share resistance genes through plasmids—small circular DNA molecules transferred between cells via conjugation. A single resistant bacterium can transfer resistance to multiple species, even across different bacterial families. Transposons (jumping genes) can move resistance genes between plasmids and chromosomes, facilitating resistance spread within and between bacteria. This genetic mobility means resistance can spread far beyond the initial antibiotic-exposed population.

Inappropriate antibiotic use drives resistance evolution. Overprescription for viral infections (where antibiotics are ineffective) exposes bacteria unnecessarily, selecting for resistant strains. Incomplete treatment courses allow partially resistant bacteria to survive and multiply. Agricultural use of antibiotics as growth promoters in livestock creates vast reservoirs of resistant bacteria that can transfer resistance genes to human pathogens. In many countries, antibiotics are available without prescription, leading to widespread misuse.

Combating resistance requires coordinated action. Antibiotic stewardship programs in hospitals ensure appropriate prescribing—using narrow-spectrum antibiotics when possible, completing full treatment courses, and reserving last-resort antibiotics for truly resistant infections. Rapid diagnostic tests help identify infections requiring antibiotics versus viral illnesses. Agriculture is phasing out growth-promoter antibiotics, reserving them for treating sick animals. Researchers are developing alternatives including bacteriophages (viruses that kill bacteria), antimicrobial peptides, and drugs that disable bacterial virulence without killing them (potentially reducing selection pressure for resistance). However, success requires global cooperation since resistant bacteria cross borders freely through travel and trade.

18. The World Health Organization warns that without action against antibiotic resistance:
 - A. All bacteria will die

- B. New antibiotics will appear naturally
 - C. Resistance will disappear
 - D. Common infections could become untreatable
19. Mutations in bacterial ribosomes can block the binding of:
- A. Tetracycline
 - B. Penicillin
 - C. All antibiotics equally
 - D. No antibiotics
20. Beta-lactamases destroy penicillin by:
- A. Changing DNA
 - B. Cleaving the beta-lactam ring
 - C. Building cell walls
 - D. Producing toxins
21. Efflux pumps contribute to resistance by:
- A. Producing enzymes
 - B. Altering ribosomes
 - C. Expelling antibiotics from cells
 - D. Transferring DNA
22. Plasmids are described as:
- A. Small circular DNA molecules
 - B. Proteins
 - C. Antibiotics
 - D. Bacterial cell walls
23. Transposons can move resistance genes between:
- A. Only viruses
 - B. Only humans
 - C. Only one bacterium
 - D. Plasmids and chromosomes
24. Overprescription of antibiotics for viral infections is problematic because:
- A. Viruses become resistant
 - B. It unnecessarily exposes bacteria, selecting for resistance
 - C. Antibiotics cure viruses
 - D. Bacteria become helpful

25. Incomplete antibiotic treatment courses allow:
- A. Complete bacterial elimination
 - B. Viral infections
 - C. Partially resistant bacteria to survive
 - D. Instant cure
26. Agricultural use of antibiotics as growth promoters:
- A. Has no effect on resistance
 - B. Only affects plants
 - C. Eliminates all bacteria
 - D. Creates reservoirs of resistant bacteria
27. Antibiotic stewardship programs aim to:
- A. Ensure appropriate prescribing
 - B. Eliminate all antibiotics
 - C. Use antibiotics for every illness
 - D. Prevent all hospital infections
28. Rapid diagnostic tests help by:
- A. Curing all infections
 - B. Making antibiotics stronger
 - C. Identifying infections requiring antibiotics versus viral illnesses
 - D. Eliminating bacteria instantly
29. Agriculture is phasing out growth-promoter antibiotics in favor of:
- A. Using more antibiotics
 - B. Reserving them for treating sick animals
 - C. Eliminating all livestock
 - D. Increasing antibiotic doses
30. Bacteriophages are:
- A. Viruses that kill bacteria
 - B. New antibiotics
 - C. Bacterial proteins
 - D. Human cells
31. The passage suggests that drugs disabling bacterial virulence without killing bacteria might:
- A. Increase resistance immediately
 - B. Have no effect
 - C. Cure all diseases

D. Reduce selection pressure for resistance

32. Horizontal gene transfer differs from mutation because it:

- A. Never occurs
- B. Involves acquiring genes from other bacteria
- C. Only happens in humans
- D. Eliminates resistance

33. Narrow-spectrum antibiotics are preferred in stewardship programs because they:

- A. Kill all bacteria equally
- B. Are less expensive only
- C. Target specific bacteria
- D. Work faster

34. Success in combating resistance requires global cooperation because:

- A. Resistant bacteria cross borders through travel and trade
- B. Antibiotics only work locally
- C. Bacteria cannot travel
- D. Each country has unique bacteria

PASSAGE III

Sleep, long dismissed as passive downtime, is now recognized as an active, essential biological process critical for physical health, cognitive function, and emotional regulation. Adults require 7-9 hours nightly, yet modern lifestyles increasingly interfere with both sleep quantity and quality. Understanding sleep's functions and consequences of deprivation has become a public health priority as chronic sleep restriction affects substantial portions of the population.

Sleep architecture involves cycling through distinct stages, each serving specific functions. Non-REM sleep progresses through stages N1 (light sleep transition), N2 (body temperature drops, heart rate slows), and N3 (deep sleep essential for physical restoration and growth hormone release). REM (rapid eye movement) sleep features vivid dreams, temporary muscle paralysis, and intense brain activity crucial for memory consolidation and emotional processing. A complete sleep cycle lasts approximately 90 minutes, with 4-6 cycles occurring per night. Early night features more deep sleep, while REM sleep dominates later cycles.

Sleep serves multiple critical functions only recently appreciated. Memory consolidation occurs primarily during sleep, with different stages processing different memory types—declarative memories (facts and events) consolidate during REM sleep, while procedural memories (skills and habits) strengthen during N2 sleep. The glymphatic system, discovered in 2012, clears metabolic

waste from the brain during sleep, including beta-amyloid proteins that accumulate in Alzheimer's disease. Sleep regulates immune function, with sleep-deprived individuals showing reduced antibody responses to vaccines and increased infection susceptibility. Hormonal regulation depends on sleep—insufficient sleep disrupts leptin and ghrelin, hormones controlling hunger and satiety, contributing to obesity risk.

Chronic sleep deprivation produces widespread health consequences. Cardiovascular disease risk increases as sleep restriction elevates blood pressure and inflammation. Diabetes risk rises as sleep loss impairs glucose metabolism and insulin sensitivity. Cognitive performance declines across attention, working memory, and decision-making. Emotional regulation deteriorates, increasing depression and anxiety risk. Even modest sleep restriction (6 hours nightly versus 8) accumulates "sleep debt" impairing performance comparable to complete sleep deprivation. Remarkably, people often fail to recognize their own impairment, believing they adapt to restricted sleep when objective measures show continued deterioration.

Improving sleep requires addressing multiple factors. Sleep hygiene practices include consistent sleep-wake schedules (even weekends), dark and cool bedrooms, and avoiding screens before bed (blue light suppresses melatonin). Caffeine and alcohol interfere with sleep architecture despite alcohol's sedative effects. Exercise improves sleep quality but timing matters—exercising too close to bedtime can be stimulating. For persistent insomnia, cognitive behavioral therapy for insomnia (CBT-I) proves more effective long-term than sleeping pills, addressing underlying thoughts and behaviors perpetuating sleep problems. Society-level changes including later school start times for adolescents and limiting shift work schedules could improve population sleep health substantially.

35. Adults require how many hours of sleep nightly?

- A. 5-6 hours
- B. 6-7 hours
- C. 8-10 hours
- D. 7-9 hours

36. Stage N3 deep sleep is essential for:

- A. Dreams only
- B. Eye movement
- C. Physical restoration and growth hormone release
- D. Wakefulness

37. REM sleep features:

- A. No brain activity
- B. Vivid dreams and temporary muscle paralysis
- C. Deep physical rest only

D. No eye movement

38. A complete sleep cycle lasts approximately:

- A. 90 minutes
- B. 60 minutes
- C. 30 minutes
- D. 120 minutes

39. Declarative memories (facts and events) consolidate primarily during:

- A. N1 sleep
- B. N2 sleep
- C. Deep sleep only
- D. REM sleep

40. The glymphatic system, discovered in 2012, functions to:

- A. Produce dreams
- B. Regulate temperature
- C. Clear metabolic waste from the brain
- D. Control breathing

41. Sleep-deprived individuals show:

- A. Enhanced immune responses
- B. Reduced antibody responses to vaccines
- C. No immune changes
- D. Immediate illness

42. Insufficient sleep disrupts leptin and ghrelin, hormones that control:

- A. Blood pressure
- B. Immune function
- C. Vision
- D. Hunger and satiety

43. Chronic sleep restriction elevates cardiovascular disease risk by:

- A. Increasing blood pressure and inflammation
- B. Decreasing heart rate only
- C. Improving circulation
- D. Reducing cholesterol

44. Sleep loss impairs glucose metabolism and insulin sensitivity, increasing risk for:

- A. Enhanced energy

- B. Improved metabolism
- C. Diabetes
- D. Better digestion

45. People with chronic sleep restriction often:

- A. Accurately assess their impairment
- B. Sleep more naturally
- C. Have no impairment
- D. Fail to recognize their own impairment

46. Blue light from screens before bed:

- A. Improves sleep
- B. Suppresses melatonin
- C. Has no effect
- D. Increases melatonin

47. Alcohol's effect on sleep architecture involves:

- A. No interference
- B. Perfect sleep quality
- C. Interfering with sleep despite sedative effects
- D. Only benefits

48. Cognitive behavioral therapy for insomnia (CBT-I) compared to sleeping pills is:

- A. More effective long-term
- B. Less effective
- C. Identical
- D. Ineffective

49. Exercising too close to bedtime can be:

- A. The best timing
- B. Sedating always
- C. Neutral
- D. Stimulating

50. Society-level changes that could improve population sleep include:

- A. Earlier school start times
- B. More shift work
- C. Later school start times for adolescents
- D. Eliminating all schedules

Quantitative Reasoning

1. What is the circumference of a circle with radius 7 cm? (Use $\pi \approx 3.14$)
 - A. 21.98 cm
 - B. 38.48 cm
 - C. 43.96 cm
 - D. 49.00 cm
2. Solve for x: $7x + 5 = 40$
 - A. 5
 - B. 7
 - C. 6
 - D. 8
3. What is $7/10 - 1/5$?
 - A. $6/10$
 - B. $1/2$
 - C. $3/5$
 - D. $2/5$
4. If a triangle has angles measuring 45° , 60° , and x° , what is x?
 - A. 85°
 - B. 70°
 - C. 75°
 - D. 80°
5. What is the area of a rectangle with length 12 cm and width 7 cm?
 - A. 38 cm^2
 - B. 84 cm^2
 - C. 72 cm^2
 - D. 96 cm^2
6. Solve the inequality: $6x - 4 > 32$
 - A. $x > 4$
 - B. $x > 5$
 - C. $x < 6$
 - D. $x > 6$
7. What is the value of $3^3 - 2^3$?
 - A. 1

- B. 27
- C. 19
- D. 35

8. If 40% of a number is 80, what is the number?

- A. 200
- B. 32
- C. 120
- D. 160

9. What is the median of the set {20, 14, 18, 22, 16}?

- A. 16
- B. 18
- C. 20
- D. 22

10. A car travels 420 miles in 7 hours. What is its average speed?

- A. 50 mph
- B. 55 mph
- C. 70 mph
- D. 60 mph

11. What is $\frac{2}{3} + \frac{1}{6}$?

- A. $\frac{3}{9}$
- B. $\frac{1}{2}$
- C. $\frac{5}{6}$
- D. $\frac{3}{6}$

12. What is the slope of a line passing through points (4, 9) and (6, 15)?

- A. 3
- B. 2
- C. 4
- D. 1

13. What is $|-18| - |6|$?

- A. 24
- B. -12
- C. -24
- D. 12

14. If $\frac{8}{x} = \frac{24}{36}$, what is x ?
- A. 10
 - B. 11
 - C. 13
 - D. 12
15. What is the surface area of a cube with edge length 5 cm?
- A. 100 cm^2
 - B. 125 cm^2
 - C. 150 cm^2
 - D. 75 cm^2
16. Solve the system: $x + y = 18$ and $x - y = 6$
- A. $x = 10, y = 8$
 - B. $x = 12, y = 6$
 - C. $x = 14, y = 4$
 - D. $x = 11, y = 7$
17. What is $\tan 45^\circ$?
- A. 1
 - B. $\frac{\sqrt{2}}{2}$
 - C. $\frac{\sqrt{3}}{2}$
 - D. $\frac{1}{2}$
18. If a rectangle has area 108 cm^2 and length 12 cm, what is its width?
- A. 7 cm
 - B. 8 cm
 - C. 10 cm
 - D. 9 cm
19. What is the least common multiple (LCM) of 12 and 18?
- A. 6
 - B. 24
 - C. 36
 - D. 72
20. A bag contains 4 red balls and 8 blue balls. What is the probability of drawing a red ball?
- A. $\frac{1}{2}$
 - B. $\frac{1}{3}$
 - C. $\frac{2}{3}$

D. $\frac{1}{4}$

21. What is the distance between points (3, 6) and (7, 9)?

- A. 3
- B. 4
- C. 7
- D. 5

22. If y varies directly as x , and $y = 30$ when $x = 6$, what is y when $x = 8$?

- A. 40
- B. 36
- C. 48
- D. 32

23. What is $\cos 60^\circ$?

- A. $\frac{\sqrt{3}}{2}$
- B. $\frac{\sqrt{2}}{2}$
- C. $\frac{1}{2}$
- D. 1

24. If a square has perimeter 48 cm, what is its area?

- A. 12 cm^2
- B. 144 cm^2
- C. 24 cm^2
- D. 96 cm^2

25. Evaluate: $f(x) = 6x - 11$ when $x = 5$

- A. 19
- B. 29
- C. 25
- D. 21

26. What is $\frac{5}{8}$ expressed as a percentage?

- A. 58%
- B. 62.5%
- C. 50%
- D. 68%

27. Solve for x : $5x + 8 = 3x + 24$

- A. 6

- B. 7
- C. 9
- D. 8

28. What is the volume of a rectangular prism with dimensions $5 \text{ cm} \times 6 \text{ cm} \times 8 \text{ cm}$?

- A. 240 cm^3
- B. 200 cm^3
- C. 180 cm^3
- D. 220 cm^3

29. What is the greatest common factor (GCF) of 42 and 56?

- A. 7
- B. 21
- C. 14
- D. 28

30. A triangle has angles measuring 50° , 65° , and x° . What is x ?

- A. 55°
- B. 60°
- C. 70°
- D. 65°

31. What is the value of $6^2 + 4^2$?

- A. 36
- B. 40
- C. 48
- D. 52

32. Simplify: $\frac{3}{4} - \frac{1}{8}$

- A. $\frac{2}{8}$
- B. $\frac{1}{2}$
- C. $\frac{5}{8}$
- D. $\frac{3}{8}$

33. A cylinder has radius 4 cm and height 9 cm. What is its volume? (Use $\pi \approx 3.14$)

- A. 301.44 cm^3
- B. 452.16 cm^3
- C. 400 cm^3
- D. 500 cm^3

34. What is 35 increased by 40%?
- A. 40
 - B. 45
 - C. 47
 - D. 49
35. If $\tan \theta = \sqrt{3}$, what is θ in degrees ($0^\circ < \theta < 90^\circ$)?
- A. 60°
 - B. 45°
 - C. 30°
 - D. 90°
36. Solve: $3(x - 4) = 2x + 7$
- A. 15
 - B. 17
 - C. 19
 - D. 21
37. What is the range of the dataset: {15, 28, 20, 35, 22}?
- A. 15
 - B. 20
 - C. 22
 - D. 28
38. If $x^2 = 144$, what are the possible values of x ?
- A. 12 only
 - B. -12 only
 - C. 72
 - D. ± 12
39. What is $\sin 30^\circ$?
- A. $1/2$
 - B. $\sqrt{2}/2$
 - C. $\sqrt{3}/2$
 - D. 1
40. Simplify: $(12x^5y^4)/(3x^3y^2)$
- A. $4x^2y$
 - B. $9x^2y^2$
 - C. $4x^2y^2$

D. $6xy^2$

Answer Explanations - Practice Test 5

Survey Of Natural Sciences

BIOLOGY (Questions 1-40)

1. Correct Answer: C (Lysosome)

Lysosomes are membrane-bound organelles containing digestive enzymes (hydrolases) that break down cellular waste, worn-out organelles, and foreign materials engulfed by the cell. These enzymes function optimally in the acidic environment maintained within lysosomes. Ribosomes synthesize proteins, peroxisomes break down fatty acids and detoxify substances, and the Golgi apparatus modifies and packages proteins.

2. Correct Answer: B (Right atrium)

The sinoatrial (SA) node, the heart's natural pacemaker, is located in the wall of the right atrium near the entrance of the superior vena cava. It generates electrical impulses that initiate each heartbeat and set the heart's rhythm, typically 60-100 beats per minute at rest.

3. Correct Answer: D (S phase)

DNA replication occurs during the S phase (synthesis phase) of the cell cycle. During this phase, the entire genome is duplicated, resulting in identical sister chromatids joined at the centromere. The G1 phase is for cell growth, G2 phase prepares for mitosis, and M phase is mitosis itself.

4. Correct Answer: A (Chlorophyll a)

Chlorophyll a is the primary photosynthetic pigment in plants, present in all photosynthetic organisms. It absorbs light most efficiently in the blue-violet and red portions of the spectrum while reflecting green light. Chlorophyll b, carotene, and xanthophyll are accessory pigments that absorb different wavelengths and transfer energy to chlorophyll a.

5. Correct Answer: D (Frameshift mutation)

A frameshift mutation involves the addition (insertion) or deletion of nucleotides that is not a multiple of three, shifting the reading frame of codons during translation. This typically results in a completely different amino acid sequence downstream of the mutation. Silent mutations don't change amino acids, missense mutations change one amino acid, and nonsense mutations create stop codons.

6. Correct Answer: A (Liver)

The gallbladder stores and concentrates bile that is produced by the liver. Bile contains bile salts that emulsify fats, facilitating their digestion and absorption in the small intestine. The pancreas produces digestive enzymes and hormones, the stomach digests proteins, and the spleen filters blood.

7. Correct Answer: C (Light-dependent reactions)

NADPH is produced during the light-dependent reactions of photosynthesis, specifically through the photosystems in the thylakoid membranes. NADPH serves as a reducing agent, providing high-energy electrons used in the Calvin cycle to reduce carbon dioxide into glucose. The Calvin cycle uses NADPH but doesn't produce it.

8. Correct Answer: A (Lagging strand)

Okazaki fragments are short DNA segments formed during synthesis of the lagging strand. Because DNA polymerase can only synthesize in the 5' to 3' direction, the lagging strand must be synthesized discontinuously in short fragments that are later joined by DNA ligase. The leading strand is synthesized continuously.

9. Correct Answer: D (Alpha cells)

Glucagon is secreted by alpha (α) cells in the pancreatic islets of Langerhans. Glucagon raises blood glucose levels by promoting glycogen breakdown and glucose synthesis in the liver. Beta cells secrete insulin, delta cells secrete somatostatin, and acinar cells produce digestive enzymes.

10. Correct Answer: C (Albumin)

Albumin, the most abundant plasma protein, is primarily responsible for maintaining osmotic pressure (colloid osmotic pressure) that keeps fluid in blood vessels rather than leaking into tissues. It also transports various substances including hormones, fatty acids, and drugs. Red blood cells transport oxygen, white blood cells fight infection, and fibrinogen is involved in clotting.

11. Correct Answer: B (Loop of Henle)

The vasa recta are specialized capillaries that run parallel to the Loop of Henle in the kidney medulla. They help maintain the osmotic gradient necessary for concentrating urine by allowing water and solutes to be exchanged between blood and the medullary interstitium. The glomerulus filters blood, and Bowman's capsule collects filtrate.

12. Correct Answer: A (RNA polymerase II)

In eukaryotic cells, RNA polymerase II transcribes mRNA from protein-coding genes. RNA polymerase I transcribes most ribosomal RNA genes, RNA polymerase III transcribes transfer RNA and some other small RNAs, and DNA polymerase replicates DNA.

13. Correct Answer: D (Veins)

Veins have valves that prevent backflow of blood, ensuring unidirectional flow toward the heart. These valves are especially important in the legs where blood must flow against gravity. Arteries and arterioles don't need valves because blood pressure from the heart propels blood forward, and capillaries are too small for valves.

14. Correct Answer: C (3 Na⁺ out, 2 K⁺ in)

The sodium-potassium pump (Na⁺/K⁺-ATPase) actively transports 3 sodium ions out of the cell and 2 potassium ions into the cell per ATP molecule hydrolyzed. This creates and maintains the electrochemical gradient essential for nerve impulses, muscle contraction, and other cellular processes.

15. Correct Answer: B (Urea)

Urea is the least toxic nitrogenous waste but requires the most water for excretion. Mammals excrete urea, which is less toxic than ammonia (allowing higher concentrations in blood) but more water-soluble than uric acid. Ammonia is most toxic but highly water-soluble, while uric acid is least toxic and requires minimal water but is energetically expensive to produce.

16. Correct Answer: D (Negative gene regulation)

The lac operon in bacteria is a classic example of negative gene regulation. In the absence of lactose, the lac repressor binds to the operator, blocking transcription. When lactose is present, it binds the repressor, causing it to release from the operator and allowing transcription. This is negative regulation because the default state is "off."

17. Correct Answer: C (Prevent alveolar collapse)

Surfactant in the lungs reduces surface tension in the alveoli, preventing them from collapsing during exhalation. Surfactant is produced by type II alveolar cells and is especially important for maintaining lung function. Without adequate surfactant, alveoli collapse and breathing becomes extremely difficult.

18. Correct Answer: C (Meiosis)

Meiosis produces four non-identical haploid cells (gametes) from one diploid cell through two successive divisions. Crossing over and independent assortment during meiosis I create genetic variation. Mitosis produces two identical diploid cells, binary fission is bacterial division, and budding is asexual reproduction.

19. Correct Answer: B (Progesterone)

The corpus luteum, formed from the ruptured follicle after ovulation, secretes primarily progesterone (and some estrogen). Progesterone prepares and maintains the uterine lining for potential pregnancy. If fertilization doesn't occur, the corpus luteum degenerates, progesterone levels drop, and menstruation begins. FSH and LH are pituitary hormones.

20. Correct Answer: A (V(D)J recombination)

Antibody diversity is generated primarily through V(D)J recombination, a process where different V (variable), D (diversity), and J (joining) gene segments are randomly combined during B cell development. This combinatorial joining, along with junctional diversity and somatic hypermutation, creates billions of different antibody specificities from a limited number of genes.

21. Correct Answer: D (Central vacuole)

The central vacuole in plant cells is responsible for turgor pressure—the pressure of cell contents against the cell wall. When filled with water, the vacuole pushes against the cell wall, making the cell rigid and supporting the plant structure. The cell wall provides structural support but doesn't create pressure, chloroplasts perform photosynthesis, and the nucleus contains DNA.

22. Correct Answer: C (Acetylcholinesterase)

Acetylcholinesterase is the enzyme that breaks down (hydrolyzes) the neurotransmitter acetylcholine in the synaptic cleft, terminating the signal. This rapid degradation allows for precise control of muscle contraction and nerve signaling. Monoamine oxidase and CATMT degrade other neurotransmitters.

23. Correct Answer: B (Troponin)

In muscle contraction, calcium ions bind to troponin, a regulatory protein on thin filaments. This binding causes a conformational change in troponin, which moves tropomyosin away from myosin-binding sites on actin, allowing cross-bridge formation and muscle contraction. Actin and myosin are the contractile proteins themselves.

24. Correct Answer: C (LH)

Luteinizing hormone (LH) stimulates ovulation—the release of the mature egg from the ovarian follicle. The LH surge, occurring mid-cycle, triggers final oocyte maturation and follicle rupture. FSH stimulates follicle development, estrogen is produced by developing follicles, and progesterone is secreted after ovulation.

25. Correct Answer: B (Inner mitochondrial membrane)

The electron transport chain in cellular respiration is located in the inner mitochondrial membrane. Here, protein complexes transfer electrons and pump protons to create the gradient used for ATP synthesis. Glycolysis occurs in the cytoplasm, and the Krebs cycle occurs in the mitochondrial matrix.

26. Correct Answer: B (Plasma cells)

Plasma cells, which are differentiated B lymphocytes, are responsible for producing and secreting antibodies. When B cells encounter their specific antigen, they proliferate and differentiate into

plasma cells that produce large quantities of antibodies. T lymphocytes mediate cell-mediated immunity, macrophages engulf pathogens, and NK cells kill infected cells.

27. Correct Answer: A (Myelinated axons)

Nodes of Ranvier are gaps in the myelin sheath found along myelinated axons. At these nodes, the axon membrane is exposed, allowing action potentials to "jump" from node to node (saltatory conduction), greatly increasing the speed of nerve impulse transmission. Unmyelinated axons lack these structures.

28. Correct Answer: D (Cell cycle progression)

Cyclin-dependent kinases (CDKs) are enzymes that regulate cell cycle progression by phosphorylating target proteins at specific checkpoints. CDKs are activated by binding to cyclins, and different cyclin-CDK complexes control transitions between cell cycle phases (G1 to S, G2 to M). This regulation ensures proper cell division.

29. Correct Answer: C (Carina)

The trachea divides into the left and right main bronchi at the carina, a ridge of cartilage located at the level of the sternal angle (approximately the 4th-5th thoracic vertebra). The larynx is the voice box above the trachea, the pharynx is the throat, and the epiglottis covers the larynx during swallowing.

30. Correct Answer: B (ATP)

ATP (adenosine triphosphate) directly provides energy for muscle contraction. When ATP is hydrolyzed to ADP and inorganic phosphate, energy is released that powers myosin head movement along actin filaments. Glucose and creatine phosphate can replenish ATP but don't directly power contraction.

31. Correct Answer: D (Meselson and Stahl)

Meselson and Stahl demonstrated the semiconservative model of DNA replication in their famous 1958 experiment using nitrogen isotopes. They showed that each new DNA molecule consists of one original strand and one newly synthesized strand, confirming Watson and Crick's prediction. Watson and Crick proposed the DNA structure, Franklin provided X-ray data, and Chargaff discovered base pairing rules.

32. Correct Answer: A (Estrogen)

The proliferative phase of the menstrual cycle (days 6-14) is stimulated by estrogen secreted by developing ovarian follicles. During this phase, the endometrium thickens and becomes highly vascularized in preparation for potential implantation. Progesterone dominates the secretory phase after ovulation.

33. Correct Answer: C (Jejunum and ileum)

The majority of nutrient absorption occurs in the jejunum and ileum, the second and third portions of the small intestine. These regions have extensive surface area due to villi and microvilli. While some absorption begins in the duodenum and the stomach absorbs some substances, most nutrient absorption happens in the jejunum and ileum. The large intestine primarily absorbs water.

34. Correct Answer: B (RNA processing)

Alternative splicing occurs during RNA processing (post-transcriptional modification) in the nucleus. Different combinations of exons are joined together while introns are removed, allowing a single gene to produce multiple protein variants. This greatly increases protein diversity without expanding genome size.

35. Correct Answer: A (Optic nerve exits the retina)

The blind spot in the eye is located where the optic nerve exits the retina to carry visual information to the brain. This region lacks photoreceptors (rods and cones), creating a gap in the visual field. We don't normally notice it because the brain fills in missing information and the blind spots of each eye don't overlap.

36. Correct Answer: D (Helicase)

Helicase is the enzyme that breaks the hydrogen bonds between DNA base pairs, unwinding the double helix during replication. This creates the replication fork where DNA synthesis occurs. DNA polymerase synthesizes new strands, ligase joins DNA fragments, and primase synthesizes RNA primers.

37. Correct Answer: C (Blood cell production)

Red bone marrow is primarily responsible for hematopoiesis—the production of blood cells including red blood cells, white blood cells, and platelets. Red marrow is found in flat bones (skull, ribs, sternum, pelvis) and ends of long bones. Yellow marrow stores fat, and mineral storage occurs in bone matrix.

38. Correct Answer: B (Sarcomeres)

The Z-line (Z-disc) is a component of sarcomeres, the contractile units of striated muscle (skeletal and cardiac). Z-lines define the boundaries of sarcomeres, anchoring thin (actin) filaments. The distance between Z-lines shortens during muscle contraction as thick and thin filaments slide past each other.

39. Correct Answer: D (Collecting duct)

Antidiuretic hormone (ADH, also called vasopressin) increases water reabsorption in the collecting duct of the kidney nephron. ADH makes the collecting duct more permeable to water by inserting aquaporin channels, allowing more water to be reabsorbed from urine back into blood, concentrating the urine. This helps maintain blood volume and osmolarity.

40. Correct Answer: A (0.42)

In Hardy-Weinberg equilibrium, if the frequency of allele A is $p = 0.7$, then the frequency of allele a is $q = 1 - 0.7 = 0.3$. The frequency of heterozygotes (Aa) is $2pq = 2(0.7)(0.3) = 0.42$ or 42%. The frequencies are: $AA = p^2 = 0.49$, $Aa = 2pq = 0.42$, $aa = q^2 = 0.09$.

GENERAL CHEMISTRY (Questions 41-70)

41. Correct Answer: C ($1s^2 2s^2 2p^6 3s^2 3p^5$)

Chlorine has atomic number 17, meaning it has 17 electrons. Following the Aufbau principle: $1s^2$ (2 electrons), $2s^2$ (2 electrons), $2p^6$ (6 electrons), $3s^2$ (2 electrons), $3p^5$ (5 electrons), totaling 17 electrons. Chlorine needs one more electron to complete its valence shell, making it highly reactive.

42. Correct Answer: B (From lowest to highest energy)

The Aufbau principle states that electrons fill orbitals from lowest to highest energy levels. Electrons occupy the lowest available energy orbital first before moving to higher energy orbitals. This follows the order: 1s, 2s, 2p, 3s, 3p, 4s, 3d, 4p, and so on.

43. Correct Answer: A (3)

The pH of a 0.001 M HCl solution is calculated using $\text{pH} = -\log[\text{H}^+]$. Since HCl is a strong acid that completely dissociates, $[\text{H}^+] = 0.001 \text{ M} = 1 \times 10^{-3} \text{ M}$. Therefore, $\text{pH} = -\log(10^{-3}) = 3$. This represents an acidic solution.

44. Correct Answer: D (HF)

Among these compounds, HF (hydrogen fluoride) has the highest boiling point due to strong hydrogen bonding. Fluorine is the most electronegative element, creating particularly strong hydrogen bonds. While H_2O also exhibits hydrogen bonding, HF's hydrogen bonds are stronger. CH_4 has only weak London dispersion forces, and NH_3 has weaker hydrogen bonds than HF.

45. Correct Answer: B (Reduced)

In the reaction $2\text{H}_2 + \text{O}_2 \rightarrow 2\text{H}_2\text{O}$, oxygen is reduced because it gains electrons (its oxidation state decreases from 0 to -2). Hydrogen is oxidized (oxidation state increases from 0 to +1). Remember: reduction is gain of electrons, oxidation is loss of electrons (OIL RIG).

46. Correct Answer: C (18)

The maximum number of electrons in an energy level is calculated using $2n^2$, where n is the principal quantum number. For $n = 3$: $2(3)^2 = 2(9) = 18$ electrons maximum. These fill the 3s (2 electrons), 3p (6 electrons), and 3d (10 electrons) subshells.

47. Correct Answer: D (Magnetic (m))

The magnetic quantum number (m_l) describes the orientation of an orbital in space. It can have integer values from $-l$ to $+l$, where l is the angular momentum quantum number. For example, p orbitals ($l = 1$) have three orientations ($m = -1, 0, +1$) corresponding to p_x , p_y , and p_z .

48. Correct Answer: A (pK_a)

A buffer solution is most effective when pH equals pK_a of the weak acid component. This is when the concentrations of weak acid and conjugate base are equal, providing maximum buffering capacity according to the Henderson-Hasselbalch equation: $pH = pK_a + \log([A^-]/[HA])$.

49. Correct Answer: B ($PV = nRT$)

The ideal gas law is represented by $PV = nRT$, where P is pressure, V is volume, n is moles of gas, R is the gas constant, and T is temperature in Kelvin. This equation combines Boyle's Law, Charles's Law, and Avogadro's Law into one relationship.

50. Correct Answer: C (+5)

In HNO_3 (nitric acid), hydrogen has oxidation state $+1$ and oxygen has -2 . Using the rule that the sum equals 0 for a neutral molecule: $(+1) + N + 3(-2) = 0$, which gives $1 + N - 6 = 0$, so $N = +5$. This is nitrogen's maximum oxidation state.

51. Correct Answer: A (Path independent)

Hess's Law states that the enthalpy change of a reaction is path independent—it depends only on the initial and final states, not the pathway taken. This means the total enthalpy change for a reaction is the same whether it occurs in one step or multiple steps. This property allows calculation of enthalpy changes for reactions that are difficult to measure directly.

52. Correct Answer: D (146.25 g)

The mass is calculated using: $mass = moles \times molar\ mass = 2.5\ moles \times 58.5\ g/mol = 146.25\ g$. This tests understanding of the relationship between moles, mass, and molar mass.

53. Correct Answer: B (F)

Fluorine (F) has the smallest atomic radius among these elements. Atomic radius decreases across a period (left to right) due to increasing nuclear charge pulling electrons closer, and increases down a group. Fluorine is in the top right of the periodic table (excluding noble gases), giving it the smallest radius. Na and K are larger alkali metals, and Cl is below F in the same group.

54. Correct Answer: C (Decreased solubility with common ions)

The common ion effect describes the decreased solubility of a salt when a common ion is added to the solution. For example, adding NaCl to a saturated AgCl solution decreases AgCl solubility

because the common Cl^- ion shifts the equilibrium toward the solid according to Le Chatelier's principle.

55. Correct Answer: A (< 0)

In the Gibbs free energy equation $\Delta G = \Delta H - T\Delta S$, a spontaneous reaction has $\Delta G < 0$ (negative). When ΔG is negative, the reaction proceeds spontaneously in the forward direction. $\Delta G = 0$ indicates equilibrium, and $\Delta G > 0$ indicates a nonspontaneous reaction.

56. Correct Answer: D (2 M)

Molarity (M) is calculated as moles of solute divided by liters of solution: $M = 4 \text{ moles} / 2 \text{ liters} = 2 \text{ M}$. This represents the molar concentration of the solution.

57. Correct Answer: C (End-to-end orbital overlap)

Sigma (σ) bonds are formed by end-to-end overlap of atomic orbitals along the internuclear axis. This can involve s-s, s-p, or p-p orbital overlap. Pi (π) bonds form from side-by-side (parallel) overlap of p orbitals. Sigma bonds are stronger and allow free rotation, while pi bonds restrict rotation.

58. Correct Answer: B (Low K_a)

A weak acid has a low K_a (acid dissociation constant), indicating that it does not dissociate completely in solution. Strong acids have high K_a values. The lower the K_a , the weaker the acid and the less it ionizes in water.

59. Correct Answer: D (1/8)

For a radioactive substance with half-life of 20 years, after 60 years (3 half-lives), the fraction remaining is $(1/2)^3 = 1/8$. After one half-life (20 years), $1/2$ remains. After two half-lives (40 years), $1/4$ remains. After three half-lives (60 years), $1/8$ remains.

60. Correct Answer: A (Fluorine)

Fluorine is the most electronegative element with a Pauling electronegativity of 4.0. Electronegativity increases across a period from left to right and decreases down a group. Fluorine, in the top right of the periodic table, has the highest electronegativity. Oxygen (3.5), nitrogen (3.0), and chlorine (3.0) are also highly electronegative but less than fluorine.

61. Correct Answer: C (Trigonal pyramidal)

The molecular geometry of ammonia (NH_3) is trigonal pyramidal. The nitrogen atom has four electron groups (three bonding pairs with hydrogen and one lone pair). According to VSEPR theory, these arrange in a tetrahedral electron geometry, but the molecular geometry considering only atoms is trigonal pyramidal with bond angles of approximately 107° .

62. Correct Answer: B (Cathode)

In a galvanic (voltaic) cell, reduction occurs at the cathode (positive electrode). Electrons flow from the anode to the cathode through the external circuit, and reduction (gain of electrons) happens at the cathode. Oxidation occurs at the anode. Remember: "An Ox, Red Cat" (Anode Oxidation, Reduction Cathode).

63. Correct Answer: D (atm·L/(mol·K))

The units of the gas constant R are atm·L/(mol·K) when using pressure in atmospheres, volume in liters, amount in moles, and temperature in Kelvin. The value is $R = 0.0821$ atm·L/(mol·K). Other unit combinations are possible (e.g., J/(mol·K)) depending on the units used in the ideal gas law.

64. Correct Answer: A (Neutrons)

Isotopes are atoms of the same element that differ in the number of neutrons. They have the same number of protons (which defines the element) and electrons (in neutral atoms) but different mass numbers due to different neutron counts. For example, carbon-12 and carbon-14 are isotopes with 6 and 8 neutrons respectively.

65. Correct Answer: C (Rate = k)

The rate law for a zero-order reaction is $\text{Rate} = k$, where the rate is independent of reactant concentration. The concentration doesn't appear in the rate law because the reaction rate is constant until the reactant is depleted. First-order is $\text{Rate} = k[A]$, and second-order is $\text{Rate} = k[A]^2$.

66. Correct Answer: D (HSO₄⁻)

The conjugate base of H₂SO₄ (sulfuric acid) is HSO₄⁻ (hydrogen sulfate or bisulfate ion). When an acid donates a proton (H⁺), what remains is its conjugate base. $\text{H}_2\text{SO}_4 \rightarrow \text{H}^+ + \text{HSO}_4^-$. HSO₄⁻ can further dissociate to SO₄²⁻, which is the conjugate base of HSO₄⁻.

67. Correct Answer: A (Electrons)

Resonance structures differ in the placement (distribution) of electrons, specifically pi electrons and lone pairs. The atoms themselves remain in the same positions. Resonance is a way of representing the delocalization of electrons in molecules where a single Lewis structure is inadequate. The actual structure is a hybrid of all resonance forms.

68. Correct Answer: D (Halves the pressure)

According to Boyle's Law, at constant temperature, pressure and volume are inversely proportional: $P_1V_1 = P_2V_2$. If volume is doubled ($V_2 = 2V_1$) while temperature remains constant, pressure is halved ($P_2 = P_1/2$). This demonstrates the inverse relationship between pressure and volume.

69. Correct Answer: B (0)

The oxidation number of an element in its standard state (uncombined form) is zero. For example, O_2 , N_2 , H_2 , and pure metallic elements like Fe or Cu all have oxidation states of 0. This is one of the fundamental rules for assigning oxidation numbers.

70. Correct Answer: C (Freezing point depression)

Freezing point depression is the colligative property used in automotive antifreeze. Adding ethylene glycol (or other solutes) to water lowers the freezing point, preventing the coolant from freezing in cold weather. Boiling point elevation is also utilized, raising the boiling point to prevent overheating.

ORGANIC CHEMISTRY (Questions 71-100)

71. Correct Answer: D (C_nH_{2n})

The general formula for alkenes is C_nH_{2n} , where n is the number of carbon atoms. Alkenes contain one carbon-carbon double bond. For example, ethene is C_2H_4 ($n=2$: C_2H_4), propene is C_3H_6 . Alkanes are C_nH_{2n+2} , and alkynes are C_nH_{2n-2} .

72. Correct Answer: A (-CHO)

The functional group present in aldehydes is -CHO (a carbonyl group bonded to a hydrogen and a carbon). The aldehyde group is always at the end of a carbon chain. -COOH is carboxylic acid, -CO- between carbons is a ketone, and -OH is an alcohol.

73. Correct Answer: C (Ethanol)

The IUPAC name for CH_3CH_2OH is ethanol. This is a two-carbon alcohol. The systematic naming is: eth- (2 carbons) + -anol (alcohol) = ethanol. Methanol has 1 carbon (CH_3OH), propanol has 3 carbons, and butanol has 4 carbons.

74. Correct Answer: B (A double bond has different groups attached)

Geometric isomers (cis-trans isomers) are possible when a double bond has different groups attached to each carbon of the double bond. The restricted rotation around the double bond allows for different spatial arrangements. Free rotation would prevent distinct isomers, and four different groups on a carbon create chirality, not geometric isomerism.

75. Correct Answer: A (Hydration)

Hydration is the reaction that adds water (H and OH) across a double bond, converting an alkene to an alcohol. Acid-catalyzed hydration follows Markovnikov's rule. Hydrogenation adds H_2 , halogenation adds halogens, and dehydration removes water.

76. Correct Answer: B (Acid chloride)

Acid chlorides (acyl chlorides) are the most reactive carbonyl compounds toward nucleophilic addition. The highly electronegative chlorine makes the carbonyl carbon very electrophilic, and chloride is an excellent leaving group. Reactivity order: acid chlorides > anhydrides > aldehydes > ketones > esters > amides.

77. Correct Answer: C (Lucas reagent)

Lucas reagent (ZnCl_2 in concentrated HCl) distinguishes primary, secondary, and tertiary alcohols based on the rate at which they form alkyl chlorides, which appear as cloudiness. Tertiary alcohols react immediately, secondary alcohols react within 5 minutes, and primary alcohols don't react at room temperature. NaBH_4 and LiAlH_4 are reducing agents, and Tollens' reagent tests for aldehydes.

78. Correct Answer: A (sp)

The hybridization of carbon in acetylene (C_2H_2) is sp. Each carbon forms two sigma bonds (one C-C and one C-H) and two pi bonds (the triple bond has one sigma and two pi bonds), requiring two hybrid orbitals from sp hybridization. The molecule is linear with 180° bond angles.

79. Correct Answer: D (Hydroboration-oxidation)

Anti-Markovnikov addition is achieved using hydroboration-oxidation (BH_3 or B_2H_6 followed by $\text{H}_2\text{O}_2/\text{OH}^-$). This adds OH to the less substituted carbon of the alkene, opposite to Markovnikov's rule. $\text{H}_2\text{SO}_4/\text{H}_2\text{O}$, HBr , and HCl all follow Markovnikov's rule.

80. Correct Answer: B (Benzene)

Benzene is aromatic—it has a planar, cyclic, fully conjugated system with 6 π electrons following Hückel's rule ($4n+2$ where $n=1$). The delocalized electrons provide exceptional stability. Cyclohexene and cyclopentane are not aromatic (not fully conjugated), and 1,3-cyclohexadiene doesn't meet all criteria.

81. Correct Answer: A (Backside attack)

The $\text{S}_\text{N}2$ mechanism proceeds via backside attack of the nucleophile on the substrate, causing inversion of configuration (Walden inversion). This is a concerted, one-step mechanism where bond formation and breaking occur simultaneously. $\text{S}_\text{N}1$ reactions proceed through carbocation intermediates.

82. Correct Answer: D (The conjugate base is stabilized by resonance)

Carboxylic acids are more acidic than alcohols because the conjugate base (carboxylate anion) is stabilized by resonance. The negative charge is delocalized over two oxygen atoms, making the anion more stable. Alcohol conjugate bases (alkoxide ions) have the negative charge localized on one oxygen, providing less stability.

83. Correct Answer: C (Alkenes)

The Wittig reaction forms alkenes (C=C double bonds) from carbonyl compounds (aldehydes or ketones) and phosphorus ylides. This is a useful method for forming carbon-carbon double bonds with predictable positions. The reaction produces an alkene and a phosphine oxide byproduct.

84. Correct Answer: B (Carbocation formation)

In E1 reactions, the rate-determining step is carbocation formation from loss of the leaving group. This is a unimolecular, two-step mechanism. After the carbocation forms, a base rapidly removes a proton to form the alkene. The rate depends only on substrate concentration.

85. Correct Answer: D (NH₂⁻)

Among these options, NH₂⁻ (amide ion) is the strongest base. Base strength generally follows the inverse of acid strength. NH₃ is a weaker acid than H₂O, CH₃COOH, or HCl, so its conjugate base (NH₂⁻) is the strongest base. Weaker acids have stronger conjugate bases.

86. Correct Answer: A (Carboxylic acid and alcohol)

Esterification (Fischer esterification) is the reaction between a carboxylic acid and an alcohol in the presence of an acid catalyst to form an ester and water: RCOOH + R'OH ⇌ RCOOR' + H₂O. This is an equilibrium reaction.

87. Correct Answer: A (Four different groups attached)

A chiral carbon (stereocenter) must have four different groups attached to it. This asymmetry creates non-superimposable mirror images (enantiomers). A double bond, having only three groups, cannot be chiral. While many chiral carbons have hydrogens, it's not required.

88. Correct Answer: C (AlCl₃ catalyst)

The Friedel-Crafts alkylation uses AlCl₃ (or another Lewis acid like FeBr₃) as a catalyst to alkylate aromatic rings. The catalyst generates a carbocation from an alkyl halide, which then attacks the aromatic ring in an electrophilic aromatic substitution. NaBH₄ is a reducing agent, H₂/Pd is for hydrogenation, and KMnO₄ is an oxidizing agent.

89. Correct Answer: D (CH₃I)

Among methyl halides, CH₃I undergoes nucleophilic substitution most readily because iodide (I⁻) is the best leaving group—it's the largest, most polarizable halide and the weakest base. Leaving group ability: I⁻ > Br⁻ > Cl⁻ > F⁻.

101. Correct Answer: B (Two aldehydes or ketones)

The aldol condensation involves the reaction of two aldehydes or two ketones (or one of each) where one acts as a nucleophile (forming an enolate) and the other acts as an electrophile. The reaction forms a β-hydroxy carbonyl compound, which can dehydrate to form an α,β-unsaturated carbonyl.

102. Correct Answer: D (Atomic number)

In the Cahn-Ingold-Prelog priority rules used for R/S nomenclature, priority is based on atomic number of atoms directly attached to the stereocenter. Higher atomic number = higher priority. If atoms are the same, move outward until a difference is found.

103. Correct Answer: A (Gabriel synthesis)

Primary amines can be prepared by the Gabriel synthesis, which uses phthalimide and involves SN₂ displacement followed by hydrolysis. This method specifically produces primary amines without contamination by secondary or tertiary amines. Friedel-Crafts acylation forms ketones, and aldol/Claisen condensations form carbon-carbon bonds.

93. Correct Answer: C (Opposite optical rotations)

Enantiomers have opposite (equal and opposite) optical rotations—one rotates plane-polarized light clockwise (+), the other counterclockwise (–) by the same magnitude. They have the same molecular formula, same connectivity, and identical physical properties except for optical activity and interactions with other chiral molecules.

94. Correct Answer: B (Ketones to alkanes)

The Clemmensen reduction reduces carbonyl groups (ketones or aldehydes) to alkanes using zinc amalgam in concentrated HCl: $R_2C=O \rightarrow R_2CH_2$. This completely removes the oxygen. For example, acetone reduces to propane. The Wolff-Kishner reduction accomplishes the same transformation under basic conditions.

95. Correct Answer: A (They lack a hydrogen on the carbon bearing OH)

Tertiary alcohols cannot be oxidized (under normal conditions) because they lack a hydrogen atom on the carbon bearing the hydroxyl group. Oxidation of alcohols requires removing a hydrogen from the alcohol carbon. Primary alcohols oxidize to aldehydes/carboxylic acids, and secondary alcohols oxidize to ketones.

96. Correct Answer: C (Ortho and para positions)

Electrophilic aromatic substitution on toluene (methylbenzene) favors the ortho and para positions because the methyl group is an activating, ortho/para-directing group. The methyl group donates electrons through hyperconjugation and inductive effects, activating the ring and directing incoming electrophiles to ortho and para positions.

97. Correct Answer: B (The less substituted alkene)

The Hofmann elimination produces the less substituted alkene (anti-Zaitsev product). This occurs when bulky bases (like quaternary ammonium hydroxides) are used, favoring removal of the more accessible hydrogen. This is opposite to Zaitsev's rule, which predicts the more substituted alkene.

98. Correct Answer: A (Base-catalyzed ester hydrolysis)

Saponification is base-catalyzed ester hydrolysis, typically using NaOH or KOH, producing a carboxylate salt and alcohol: $\text{RCOOR}' + \text{OH}^- \rightarrow \text{RCOO}^- + \text{R}'\text{OH}$. This is the reaction used to make soap from fats (esters of glycerol and fatty acids). Unlike acid-catalyzed hydrolysis, saponification is irreversible.

99. Correct Answer: D (Molecular weight)

Mass spectrometry determines the molecular weight (molecular mass) of a compound by measuring the mass-to-charge ratio (m/z) of ionized molecules. The molecular ion peak (M^+) gives the molecular weight directly. Fragmentation patterns can also provide structural information, but the primary determination is molecular weight.

104. Correct Answer: B (Number of equivalent hydrogens)

In ^1H NMR spectroscopy, the integration (area under a peak) indicates the number of equivalent hydrogens producing that signal. The ratio of integrations corresponds to the ratio of hydrogens in different environments. Chemical shift indicates electronic environment, splitting pattern shows neighboring hydrogens, and peak width relates to relaxation.

Perceptual Ability Test

ANGLE DISCRIMINATION (Questions 1-15)

1. Correct Answer: C (3-2-1-4)

The angles in order from smallest to largest are: Angle 3 (38°) < Angle 2 (47°) < Angle 1 (54°) < Angle 4 (62°). This gives the sequence 3-2-1-4, correctly ranking all four angles from smallest to largest based on their degree measurements.

2. Correct Answer: B (S-Q-P-R)

The angles rank as: Angle S (52°) < Angle Q (58°) < Angle P (69°) < Angle R (75°). The sequence S-Q-P-R correctly orders these angles from smallest to largest.

3. Correct Answer: A (1-2-3-4)

The angles in order are: Angle 1 (24°) < Angle 2 (36°) < Angle 3 (42°) < Angle 4 (50°). This ranking correctly sequences the four angles from smallest to largest, which are already in numerical order.

4. Correct Answer: D (B-D-A-C)

The angles rank as: Angle B (74°) < Angle D (79°) < Angle A (81°) < Angle C (87°). The sequence B-D-A-C correctly orders these angles from smallest to largest.

5. Correct Answer: B (X-Y-W-Z)

Angle W = 60° (two-thirds of 90°), Angle X = 48° , Angle Y = 56° , Angle Z = 72° . Ordering from smallest to largest: X (48°) < Y (56°) < W (60°) < Z (72°). The sequence X-Y-W-Z is the correct ascending order.

6. Correct Answer: A (1-2-3-4)

The angles rank as: Angle 1 (15°) < Angle 2 (29°) < Angle 3 (36°) < Angle 4 (43°). This sequence correctly orders the angles from smallest to largest, which are already in numerical order.

7. Correct Answer: B (O-M-P-N)

The angles in order are: Angle O (55°) < Angle M (61°) < Angle P (68°) < Angle N (73°). The sequence O-M-P-N correctly ranks these angles.

8. Correct Answer: D (1-3-2-4)

The angles rank as: Angle 1 (20°) < Angle 3 (27°) < Angle 2 (32°) < Angle 4 (39°). This sequence correctly orders the angles from smallest to largest.

9. Correct Answer: A (C-A-B-D)

The angles in order are: Angle C (35°) < Angle A (46°) < Angle B (52°) < Angle D (64°). The sequence C-A-B-D correctly ranks these angles.

10. Correct Answer: C (2-4-1-3)

The angles rank as: Angle 2 (63°) < Angle 4 (66°) < Angle 1 (70°) < Angle 3 (77°). This sequence correctly orders the angles from smallest to largest.

11. Correct Answer: B (W-Z-Y-X)

The angles in order are: Angle W (33°) < Angle Z (40°) < Angle Y (45°) < Angle X (51°). The sequence W-Z-Y-X correctly ranks these angles from smallest to largest.

12. Correct Answer: B (1-2-3-4)

The angles rank as: Angle 1 (17°) < Angle 2 (25°) < Angle 3 (31°) < Angle 4 (44°). This sequence correctly orders all four angles from smallest to largest, which are already in numerical order.

13. Correct Answer: C (Q-S-P-R)

The angles in order are: Angle Q (49°) < Angle S (54°) < Angle P (67°) < Angle R (78°). The sequence Q-S-P-R correctly ranks these angles.

14. Correct Answer: A (1-3-2-4)

The angles rank as: Angle 1 (26°) < Angle 3 (34°) < Angle 2 (40°) < Angle 4 (48°). This sequence correctly orders the angles from smallest to largest.

15. Correct Answer: D (D-A-B-C)

The angles in order are: Angle D (71°) < Angle A (76°) < Angle B (84°) < Angle C (89°). The sequence D-A-B-C correctly ranks these angles from smallest to largest.

PAPER FOLDING (Questions 16-30)

16. Correct Answer: B (6)

When paper is folded in half once (creating 2 layers) and three holes are punched through both layers, unfolding reveals $3 \times 2 = 6$ total holes positioned symmetrically across the fold line.

17. Correct Answer: C (16)

Three folds create 8 layers ($2^3 = 8$). Punching 2 holes through all 8 layers produces $2 \times 8 = 16$ total holes when unfolded.

18. Correct Answer: A (1)

When a hole is punched exactly on the fold line of paper folded once, both layers are punched at the same location. When unfolded, this appears as a single hole positioned on what was the fold line.

19. Correct Answer: A (1)

When paper is folded diagonally and a hole is punched exactly on the diagonal fold line, both layers are punched at the same location. Unfolding reveals 1 hole on the diagonal.

20. Correct Answer: B (2)

When paper is folded in half once (creating 2 layers) and one hole is punched near the edge away from the fold, unfolding reveals 2 holes positioned symmetrically on each side of the fold line.

21. Correct Answer: D (8)

Three folds create 8 layers ($2^3 = 8$). One punch through all 8 layers produces 8 holes when completely unfolded, arranged in a symmetric pattern.

22. Correct Answer: A (4)

Two folds create 4 layers ($2^2 = 4$). One punch through all 4 layers produces 4 holes when unfolded, positioned symmetrically based on the two fold lines.

23. Correct Answer: C (4)

One fold creates 2 layers. Punching 2 holes through both layers produces $2 \times 2 = 4$ total holes when unfolded.

24. Correct Answer: D (4)

Two folds create 4 layers. Punching at the point where both folds meet (the center of the original paper) produces 4 holes when unfolded, clustered near the center in a symmetric pattern.

25. Correct Answer: B (6)

One fold creates 2 layers. Punching 3 holes through both layers produces $3 \times 2 = 6$ total holes when unfolded.

26. Correct Answer: A (4)

A diagonal fold creates 2 layers. Punching 2 holes away from the fold produces $2 \times 2 = 4$ holes when unfolded, positioned symmetrically across the diagonal fold line.

27. Correct Answer: C (4)

Two folds create 4 layers. Punching at an edge (not corner) produces 4 holes when unfolded, arranged along or near one edge in a symmetric pattern.

28. Correct Answer: D (8)

Two folds create 4 layers. Punching 2 holes through all 4 layers produces $2 \times 4 = 8$ total holes when unfolded.

29. Correct Answer: B (8)

One fold creates 2 layers. Punching 4 holes through both layers produces $4 \times 2 = 8$ total holes when unfolded.

30. Correct Answer: C (4)

Two folds create 4 layers. Punching a corner of the folded paper produces 4 holes when unfolded, positioned near corners or edges of the original square in a symmetric pattern.

CUBE COUNTING (Questions 31-45)

31. Correct Answer: A (1)

Interior cubes (0 faces exposed) formula: $(a-2)(b-2)(c-2) = (3-2)(3-2)(3-2) = 1 \times 1 \times 1 = 1$ completely interior cube in a $3 \times 3 \times 3$ cube.

32. Correct Answer: D (8)

Any cube or rectangular prism has exactly 8 corners. A $4 \times 4 \times 4$ cube has 8 corner cubes where 3 faces meet, giving 8 cubes with exactly 3 faces exposed.

33. Correct Answer: B (30)

A $2 \times 3 \times 5$ rectangular prism contains $2 \times 3 \times 5 = 30$ total unit cubes.

34. Correct Answer: A (2)

In a straight line of 8 cubes, the 2 end cubes each have 5 faces exposed (all faces except the one touching the adjacent cube). The 6 middle cubes each have 4 faces exposed.

35. Correct Answer: C (64)

Interior cubes (0 faces exposed) formula: $(a-2)(b-2)(c-2) = (6-2)(6-2)(6-2) = 4 \times 4 \times 4 = 64$ completely interior cubes in a $6 \times 6 \times 6$ cube.

36. Correct Answer: D (8)

Any rectangular prism has exactly 8 corners. A $3 \times 4 \times 3$ prism has 8 corner cubes with exactly 3 faces exposed.

37. Correct Answer: B (12)

Edge cubes (2 faces exposed) in a $3 \times 3 \times 3$ cube: $4[(a-2) + (b-2) + (c-2)] = 4[(3-2) + (3-2) + (3-2)] = 4[1+1+1] = 4(3) = 12$ edge cubes.

38. Correct Answer: C (24)

A $2 \times 2 \times 6$ rectangular prism contains $2 \times 2 \times 6 = 24$ total unit cubes.

39. Correct Answer: A (54)

Face cubes (1 face exposed) in a $5 \times 5 \times 5$ cube: $2[(a-2)(b-2) + (b-2)(c-2) + (a-2)(c-2)] = 2[(3)(3) + (3)(3) + (3)(3)] = 2[9+9+9] = 2(27) = 54$ face cubes.

40. Correct Answer: D (28)

A $4 \times 3 \times 3$ rectangular prism contains $4 \times 3 \times 3 = 36$ total unit cubes. Every rectangular prism has exactly 8 corner cubes. Therefore, cubes that are NOT corner cubes = $36 - 8 = 28$ cubes.

41. Correct Answer: B (5)

In a pyramid structure with specific configuration (9 bottom, 4 middle, 1 top), analyzing the exposed faces shows that approximately 5 cubes have exactly 3 faces exposed at various corner and edge positions of the pyramid structure.

42. Correct Answer: C (20)

Edge cubes (2 faces exposed) in a $3 \times 3 \times 5$ rectangular prism: $4[(a-2) + (b-2) + (c-2)] = 4[(3-2) + (3-2) + (5-2)] = 4[1+1+3] = 4(5) = 20$ cubes with exactly 2 faces exposed.

43. Correct Answer: C (3)

In an L-shaped structure with 8 total cubes (6 in a row + 2 stacked on one end), analyzing the configuration shows approximately 3 cubes have exactly 3 exposed faces at corner-like positions of the L-shape.

44. Correct Answer: D (50)

A $5 \times 5 \times 2$ rectangular prism contains $5 \times 5 \times 2 = 50$ total cubes. Since one dimension is only 2 (meaning $2 - 2 = 0$), there are no completely interior cubes. All 50 cubes have at least one face exposed.

45. Correct Answer: B (0)

A $2 \times 2 \times 2$ cube consists entirely of corner cubes. All 8 unit cubes are at corners where 3 faces meet. There are no edge cubes (which would have exactly 2 faces exposed) because edge cubes require at least one dimension ≥ 3 .

PATTERN FOLDING (Questions 46-60)

46. Correct Answer: C (Open-top cube)

Five squares in a plus/cross shape (one center, four extending from each edge) form an open-top cube when folded. One square is the bottom, four form the sides, but there's no sixth square for the top, creating a 5-sided box.

47. Correct Answer: A (Square pyramid)

A net with 1 square and 4 triangles attached to each edge of the square folds into a square pyramid. The square forms the base, and the four triangles fold upward to meet at a common apex.

48. Correct Answer: D (Triangular prism)

Two triangular faces (the ends) and 3 rectangular faces (wrapping around) form a triangular prism when folded. This is the standard net for a prism with triangular cross-section.

49. Correct Answer: B (Tetrahedron)

Four equilateral triangles in a connected arrangement can fold into a tetrahedron (triangular pyramid) where all four faces are triangles, forming a 4-faced polyhedron.

50. Correct Answer: A (Pentagonal pyramid)

A pentagon base with 5 triangles (one on each edge) folds into a pentagonal pyramid. The triangles meet at an apex above the pentagonal base.

51. Correct Answer: B (Cube)

Six squares in a T-shape (4 in a row, 1 above and 1 below the second square) is one of the standard nets for a complete cube. When folded properly, all six faces close to form a cube.

52. Correct Answer: C (Hexagonal prism)

A hexagon with 6 rectangles attached to its edges forms a hexagonal prism. The rectangles wrap around to form the sides, creating a prism with hexagonal cross-section.

53. Correct Answer: A (Partial cube / open box)

Four squares in an L-shape cannot form a complete cube (which requires 6 squares). When folded, it creates a partial box structure with some faces missing.

54. Correct Answer: D (Rectangular prism)

Six rectangles arranged appropriately fold into a rectangular prism (box shape). The rectangles form the top, bottom, and four sides.

55. Correct Answer: A (Partial pyramid / missing one face)

With only 3 triangles attached to a square base, this forms an incomplete pyramid missing one triangular face. A complete square pyramid requires 4 triangular faces plus the base.

56. Correct Answer: D (Hexagonal prism)

Two hexagonal ends connected by 6 rectangles form a complete hexagonal prism. This creates a prism with hexagonal cross-section.

57. Correct Answer: C (Tetrahedron)

One large triangle with 3 smaller triangles attached to its edges folds into a tetrahedron (triangular pyramid) with 4 triangular faces total.

58. Correct Answer: A (Cube)

Six equal squares in a cross pattern is a standard cube net. When folded, it forms a complete cube with all six faces.

59. Correct Answer: B (Irregular polyhedron)

Irregular polygons that don't match standard shapes form an irregular 3D shape when folded that doesn't fit standard categories like cubes, pyramids, or regular prisms.

60. Correct Answer: D (Open-top cube)

Three squares in a row with 1 square attached to the side of the middle square (T-shape) provides only 4 squares. This can form an open-top cube with one square as bottom and three forming three sides, leaving two sides and the top open.

APERTURES / KEYHOLES (Questions 61-75)

61. Correct Answer: C (Rectangle)

A rectangular prism (box shape) shows rectangular silhouettes from multiple angles. A rectangle is a possible aperture shape for this object when oriented appropriately to show a rectangular face.

62. Correct Answer: B (Circle or Triangle)

A cone shows a circular silhouette when viewed from the base and a triangular silhouette when viewed from the side. Both aperture shapes are possible depending on orientation.

63. Correct Answer: A (Square)

A cube can pass through a square aperture when oriented face-first. Viewing a cube from directly in front shows a square silhouette, making a square aperture the correct match.

64. Correct Answer: C (Circle)

A sphere viewed from any angle appears as a circle. Therefore, a circular aperture is the shape a sphere could pass through (assuming the aperture matches the sphere's diameter).

65. Correct Answer: D (Triangle or Rectangle)

A triangular prism shows a triangular silhouette when viewed from the end (showing the triangular face) and a rectangular silhouette when viewed from the side. Both aperture shapes work.

66. Correct Answer: A (Triangle)

A cylinder can show circle (end view), rectangle (side view), or oval (angled view) silhouettes, but never a triangular silhouette regardless of orientation. Triangle would NOT work.

67. Correct Answer: D (Square or Triangle)

A square pyramid shows a square silhouette when viewed from the base and triangular silhouettes when viewed from the sides. Both aperture shapes are possible.

68. Correct Answer: B (Hexagon or Rectangle)

A hexagonal prism shows hexagonal silhouettes from the ends and rectangular silhouettes from the sides. Both aperture shapes are possible.

69. Correct Answer: A (Triangle)

A tetrahedron has all triangular faces. From any angle, it shows a triangular silhouette, making triangle the correct aperture shape.

70. Correct Answer: C (Sphere or Cylinder)

Among the 3D objects listed, both sphere and cylinder can pass through a circular aperture. A sphere shows circles from all angles, and a cylinder shows a circle when viewed along its axis.

71. Correct Answer: D (Triangle or Square)

An octahedron has triangular faces and when viewed from certain angles can show either triangular or square silhouettes depending on orientation. Both are possible apertures.

72. Correct Answer: B (Pentagon or Rectangle)

A pentagonal prism shows pentagonal silhouettes from the ends and rectangular silhouettes from the sides. Both aperture shapes are possible.

73. Correct Answer: C (Rectangle)

A rectangular prism can produce rectangular silhouettes from certain angles, but a sphere can only produce circular silhouettes. A rectangle aperture works for the prism but NOT for the sphere.

74. Correct Answer: A (Triangle)

A cylinder positioned appropriately can show circle (end view), rectangle (side view), or oval (angled) silhouettes, but cannot produce a triangular silhouette. Triangle is NOT a possible aperture shape.

75. Correct Answer: D (Triangular prism)

A triangular prism can pass through both a triangular aperture (when oriented to show the triangular end face) and a rectangular aperture (when oriented to show the rectangular side face). The prism's geometry allows both orientations.

VIEW RECOGNITION (Questions 76-90)

76. Correct Answer: B (Square pyramid)

A square pyramid has a square top view (the base), triangular front view (showing the slant from base to apex), and triangular side view. This combination uniquely identifies a square pyramid.

77. Correct Answer: A (Cylinder)

A cylinder has a circular top view (looking down the axis), rectangular front view (showing the length and diameter), and rectangular side view. This combination uniquely identifies a cylinder.

78. Correct Answer: C (Sphere)

A sphere shows identical circular views from all three orthogonal directions (top, front, side) because it's perfectly round in all directions. Only a sphere has this property among the options.

79. Correct Answer: D (Square)

Viewing a cube from the top shows one square face directly. The top view of a cube is a square matching the face dimensions.

80. Correct Answer: B (Triangular prism)

A triangular top view with rectangular front and side views identifies a triangular prism. The top shows the triangular cross-section, while front and side show the length.

81. Correct Answer: C (Hexagonal prism)

A hexagonal top view with rectangular front and side views identifies a hexagonal prism. The prism has a hexagonal cross-section with length extending perpendicular to it.

82. Correct Answer: D (Rectangle)

Viewing a cylinder from the side (perpendicular to its axis) shows a rectangular silhouette with the length being the cylinder height and width being the diameter.

83. Correct Answer: A (Cube)

All three views (top, front, side) showing identical squares indicates a cube. Only a cube has this property where all faces are identical squares and all three orthogonal views are the same.

84. Correct Answer: C (Pentagonal prism)

A pentagonal top view with rectangular front and side views identifies a pentagonal prism. The prism has a pentagon cross-section with length extending perpendicular to it.

85. Correct Answer: B (Triangle)

Viewing a triangular prism from the end (looking directly at the triangular face) shows a triangle. This is the cross-sectional shape of the prism.

86. Correct Answer: B (Circle)

Viewing a cone from directly above (top view) shows a circle representing the circular base. The apex is at the center of this circle.

87. Correct Answer: C (Rectangular prism)

Different rectangular views (rectangle top, rectangle front, square side) indicate a rectangular prism with different length, width, and height dimensions. The square side view means two dimensions are equal.

88. Correct Answer: D (Square)

A square pyramid viewed from directly above shows a square (the base). The apex is at the center of the square, but the outline viewed from above is square.

89. Correct Answer: D (Cone)

A cone has a circular top view (looking down at the circular base), triangular front view (showing the slanted side tapering to a point), and triangular side view. This combination identifies a cone.

90. Correct Answer: A (L-shaped block structure)

An L-shaped top view with rectangular front and side views indicates an L-shaped block structure. The L-configuration is visible from above while sides show rectangular profiles.

Reading Comprehension

PASSAGE I - Blood-Brain Barrier (Questions 1-17)

1. Correct Answer: B (98%)

The passage explicitly states "approximately 98% of small-molecule drugs and virtually all large-molecule therapeutics cannot cross the BBB." This statistic emphasizes the significant challenge the blood-brain barrier poses for drug delivery to the brain.

2. Correct Answer: A (Paracellular transport)

The passage explains "Endothelial cells lining brain capillaries are connected by tight junction proteins that seal gaps between cells, preventing paracellular transport (movement between cells)." Paracellular transport refers to movement between cells, which is blocked by tight junctions.

3. Correct Answer: D (Fenestrations)

The passage states "These endothelial cells also lack fenestrations (pores) common in other capillaries." Fenestrations are small pores that allow passage of materials, and their absence in brain capillaries contributes to the barrier's selectivity.

4. Correct Answer: C (Maintain barrier properties)

The passage notes "Astrocyte end-feet wrap around capillaries, releasing signals that maintain barrier properties." Astrocytes play a supportive role in preserving the blood-brain barrier's integrity.

5. Correct Answer: B (Glucose)

The passage explicitly states "Glucose enters via GLUT1 transporters, essential amino acids use carrier-mediated transport." GLUT1 is specifically mentioned as the glucose transporter.

6. Correct Answer: D (An efflux pump)

The passage describes "efflux transporters like P-glycoprotein that pump potentially harmful substances back into the bloodstream." P-glycoprotein actively pumps substances out of the brain.

7. Correct Answer: A (Lacking a complete blood-brain barrier)

The passage states "Certain brain regions called circumventricular organs lack a complete blood-brain barrier, allowing direct monitoring of blood composition." This incomplete barrier is their defining characteristic.

8. Correct Answer: C (Detect blood toxins and trigger vomiting)

The passage notes "The area postrema, located in the brainstem, detects toxins in blood and triggers vomiting." This is the specific function of this circumventricular organ.

9. Correct Answer: B (The hypothalamus)

The passage states "The median eminence permits hormone exchange between blood and the hypothalamus." This allows hormonal communication between the bloodstream and the hypothalamus.

10. Correct Answer: A (Aids diagnosis by allowing contrast agent leakage)

The passage explains "Brain tumors often disrupt the barrier, allowing contrast agents used in MRI to leak into brain tissue, actually aiding diagnosis." The disruption paradoxically helps in detecting tumors.

11. Correct Answer: D (Immune cell infiltration)

The passage states "Multiple sclerosis involves inflammatory breakdown of the BBB, permitting immune cell infiltration that damages myelin." The barrier breakdown allows harmful immune cells to enter the brain.

12. Correct Answer: C (Weeks)

The passage notes "Traumatic brain injury can cause both immediate barrier rupture and delayed dysfunction lasting weeks." The dysfunction can persist for an extended period.

13. Correct Answer: B (Barrier breakdown)

The passage explains "Stroke creates regions where barrier breakdown allows brain edema (swelling) that worsens outcomes." The compromised barrier permits fluid accumulation.

14. Correct Answer: D (Excludes many therapeutic drugs)

The passage states "This protective mechanism, while beneficial against toxins, also excludes many therapeutic drugs designed to treat brain diseases." The efflux function has both protective and problematic consequences.

15. Correct Answer: A (Sufficiently small and uncharged)

The passage notes "lipid-soluble molecules can diffuse through endothelial cell membranes if sufficiently small and uncharged." Both conditions must be met for passive diffusion.

16. Correct Answer: B (Structural support and blood flow regulation)

The passage states "Pericytes embedded in the capillary basement membrane provide structural support and regulate blood flow." These are their dual functions.

17. Correct Answer: C (Thirst and blood pressure)

The passage notes "The subfornical organ and organum vasculosum respond to circulating signals regulating thirst and blood pressure." These are the specific physiological processes they monitor.

PASSAGE II - Antibiotic Resistance (Questions 18-34)

18. Correct Answer: D (Common infections could become untreatable)

The passage states "The World Health Organization warns that without action, common infections could become untreatable, returning medicine to the pre-antibiotic era when minor injuries could prove fatal."

19. Correct Answer: A (Tetracycline)

The passage provides the example "mutations in bacterial ribosomes can block tetracycline binding, rendering it ineffective." Tetracycline is specifically mentioned.

20. Correct Answer: B (Cleaving the beta-lactam ring)

The passage explains "beta-lactamases break down penicillin and related drugs by cleaving their beta-lactam ring structure." The enzyme destroys the critical structural component.

21. Correct Answer: C (Expelling antibiotics from cells)

The passage states "Efflux pumps actively expel antibiotics from bacterial cells before they can act." This removes the drug before it can be effective.

22. Correct Answer: A (Small circular DNA molecules)

The passage defines "plasmids—small circular DNA molecules transferred between cells via conjugation." This is the structural description of plasmids.

23. Correct Answer: D (Plasmids and chromosomes)

The passage notes "Transposons (jumping genes) can move resistance genes between plasmids and chromosomes." These mobile genetic elements facilitate gene transfer.

24. Correct Answer: B (It unnecessarily exposes bacteria, selecting for resistance)

The passage explains "Overprescription for viral infections (where antibiotics are ineffective) exposes bacteria unnecessarily, selecting for resistant strains." The exposure creates selection pressure.

25. Correct Answer: C (Partially resistant bacteria to survive)

The passage states "Incomplete treatment courses allow partially resistant bacteria to survive and multiply." This enables resistance to develop.

26. Correct Answer: D (Creates reservoirs of resistant bacteria)

The passage notes "Agricultural use of antibiotics as growth promoters in livestock creates vast reservoirs of resistant bacteria that can transfer resistance genes to human pathogens."

27. Correct Answer: A (Ensure appropriate prescribing)

The passage states "Antibiotic stewardship programs in hospitals ensure appropriate prescribing." This is their primary purpose.

28. Correct Answer: C (Identifying infections requiring antibiotics versus viral illnesses)

The passage notes "Rapid diagnostic tests help identify infections requiring antibiotics versus viral illnesses." This prevents inappropriate antibiotic use.

29. Correct Answer: B (Reserving them for treating sick animals)

The passage states "Agriculture is phasing out growth-promoter antibiotics, reserving them for treating sick animals." This represents responsible use.

30. Correct Answer: A (Viruses that kill bacteria)

The passage defines "bacteriophages (viruses that kill bacteria)" as an alternative being developed. This is their basic characteristic.

31. Correct Answer: D (Reduce selection pressure for resistance)

The passage suggests "drugs that disable bacterial virulence without killing them (potentially reducing selection pressure for resistance)." Not killing bacteria may slow resistance evolution.

32. Correct Answer: B (Involves acquiring genes from other bacteria)

The passage explains horizontal gene transfer allows "bacteria can share resistance genes through plasmids," distinguishing it from spontaneous mutation.

33. Correct Answer: C (Target specific bacteria)

Narrow-spectrum antibiotics are preferred because they "target specific bacteria" rather than killing all bacteria broadly, reducing selection pressure on non-pathogenic bacteria.

34. Correct Answer: A (Resistant bacteria cross borders through travel and trade)

The passage concludes "success requires global cooperation since resistant bacteria cross borders freely through travel and trade." This makes resistance a global problem.

PASSAGE III - Sleep (Questions 35-50)

35. Correct Answer: D (7-9 hours)

The passage states "Adults require 7-9 hours nightly." This is the recommended sleep duration for adults.

36. Correct Answer: C (Physical restoration and growth hormone release)

The passage describes "N3 (deep sleep essential for physical restoration and growth hormone release)." These are the key functions of deep sleep.

37. Correct Answer: B (Vivid dreams and temporary muscle paralysis)

The passage states "REM (rapid eye movement) sleep features vivid dreams, temporary muscle paralysis, and intense brain activity." These are characteristic REM features.

38. Correct Answer: A (90 minutes)

The passage notes "A complete sleep cycle lasts approximately 90 minutes." This is the typical duration for one complete cycle through all sleep stages.

39. Correct Answer: D (REM sleep)

The passage states "declarative memories (facts and events) consolidate during REM sleep, while procedural memories (skills and habits) strengthen during N2 sleep." REM is specified for declarative memories.

40. Correct Answer: C (Clear metabolic waste from the brain)

The passage explains "The glymphatic system, discovered in 2012, clears metabolic waste from the brain during sleep, including beta-amyloid proteins that accumulate in Alzheimer's disease."

41. Correct Answer: B (Reduced antibody responses to vaccines)

The passage states "sleep-deprived individuals showing reduced antibody responses to vaccines and increased infection susceptibility." The immune response is impaired.

42. Correct Answer: D (Hunger and satiety)

The passage notes "insufficient sleep disrupts leptin and ghrelin, hormones controlling hunger and satiety, contributing to obesity risk." These hormones regulate appetite.

43. Correct Answer: A (Increasing blood pressure and inflammation)

The passage states "Cardiovascular disease risk increases as sleep restriction elevates blood pressure and inflammation." These are the mechanisms by which sleep loss affects heart health.

44. Correct Answer: C (Diabetes)

The passage notes "Diabetes risk rises as sleep loss impairs glucose metabolism and insulin sensitivity." These metabolic changes increase diabetes risk.

45. Correct Answer: D (Fail to recognize their own impairment)

The passage states "Remarkably, people often fail to recognize their own impairment, believing they adapt to restricted sleep when objective measures show continued deterioration."

46. Correct Answer: B (Suppresses melatonin)

The passage notes "avoiding screens before bed (blue light suppresses melatonin)." Blue light interferes with the sleep-promoting hormone.

47. Correct Answer: C (Interfering with sleep despite sedative effects)

The passage states "Caffeine and alcohol interfere with sleep architecture despite alcohol's sedative effects." Alcohol may help falling asleep but disrupts sleep quality.

48. Correct Answer: A (More effective long-term)

The passage notes "cognitive behavioral therapy for insomnia (CBT-I) proves more effective long-term than sleeping pills." CBT-I provides lasting benefits.

49. Correct Answer: D (Stimulating)

The passage states "Exercise improves sleep quality but timing matters—exercising too close to bedtime can be stimulating." Late exercise can interfere with sleep onset.

50. Correct Answer: C (Later school start times for adolescents)

The passage suggests "Society-level changes including later school start times for adolescents and limiting shift work schedules could improve population sleep health substantially." Later starts align better with adolescent sleep needs.

Quantitative Reasoning

1. Correct Answer: C (43.96 cm)

The circumference of a circle is $C = 2\pi r$. With radius = 7 cm and $\pi \approx 3.14$: $C = 2 \times 3.14 \times 7 = 43.96$ cm. This formula calculates the distance around the circle.

2. Correct Answer: A (5)

Solve the equation $7x + 5 = 40$ by first subtracting 5 from both sides: $7x = 40 - 5 = 35$. Divide both sides by 7: $x = 35/7 = 5$. Verify: $7(5) + 5 = 35 + 5 = 40 \checkmark$.

3. Correct Answer: B (1/2)

To subtract fractions with different denominators, find a common denominator. The LCD of 10 and 5 is 10: $1/5 = 2/10$. Then $7/10 - 2/10 = 5/10 = 1/2$. This tests fraction subtraction with unlike denominators.

4. Correct Answer: C (75°)

In any triangle, the three angles sum to 180° . With angles 45° , 60° , and x° : $45 + 60 + x = 180$, so $105 + x = 180$, giving $x = 75^\circ$. This tests the fundamental triangle angle sum property.

5. Correct Answer: B (84 cm²)

The area of a rectangle is $A = \text{length} \times \text{width}$. With length = 12 cm and width = 7 cm: $A = 12 \times 7 = 84 \text{ cm}^2$. This is a direct application of the rectangle area formula.

6. Correct Answer: D ($x > 6$)

Solve the inequality $6x - 4 > 32$ by adding 4 to both sides: $6x > 36$. Divide both sides by 6: $x > 6$. The inequality direction remains the same because we divided by a positive number.

7. Correct Answer: C (19)

Calculate $3^3 - 2^3$: First, $3^3 = 3 \times 3 \times 3 = 27$. Then, $2^3 = 2 \times 2 \times 2 = 8$. Finally, $27 - 8 = 19$. This tests exponent evaluation and order of operations.

8. Correct Answer: A (200)

If 40% of a number equals 80, set up the equation: $0.40 \times N = 80$. Divide both sides by 0.40: $N = 80/0.40 = 200$. Alternatively, recognize that $40\% = 2/5$, so if $2/5$ of $N = 80$, then $N = 80 \times (5/2) = 200$.

9. Correct Answer: B (18)

To find the median, first arrange the numbers in order: $\{14, 16, 18, 20, 22\}$. The median is the middle value in an ordered set. With 5 values, the third value is the median: 18.

10. Correct Answer: D (60 mph)

Average speed = distance \div time = 420 miles \div 7 hours = 60 miles per hour. This straightforward calculation tests understanding of the distance-rate-time relationship.

11. Correct Answer: C (5/6)

To add fractions with different denominators, find a common denominator. The LCD of 3 and 6 is 6: $2/3 = 4/6$. Then $4/6 + 1/6 = 5/6$. This tests fraction addition with unlike denominators.

12. Correct Answer: A (3)

The slope formula is $m = (y_2 - y_1)/(x_2 - x_1)$. With points (4, 9) and (6, 15): $m = (15 - 9)/(6 - 4) = 6/2 = 3$. A slope of 3 means the line rises 3 units vertically for every 1 unit horizontally.

13. Correct Answer: D (12)

The absolute value of -18 is 18, and the absolute value of 6 is 6. Therefore, $|-18| - |6| = 18 - 6 = 12$. Absolute value represents distance from zero, always positive or zero.

14. Correct Answer: D (12)

Solve $8/x = 24/36$ by first simplifying the right side: $24/36 = 2/3$. So $8/x = 2/3$. Cross-multiply: $8 \times 3 = 2 \times x$, giving $24 = 2x$, so $x = 12$. Verify: $8/12 = 2/3 \checkmark$.

15. Correct Answer: C (150 cm²)

The surface area of a cube is $SA = 6s^2$ where s is the edge length. With $s = 5$ cm: $SA = 6 \times 5^2 = 6 \times 25 = 150$ cm². A cube has 6 identical square faces, each with area s^2 .

16. Correct Answer: B (x = 12, y = 6)

Solve the system $x + y = 18$ and $x - y = 6$ by adding the equations: $(x + y) + (x - y) = 18 + 6$, giving $2x = 24$, so $x = 12$. Substitute into the first equation: $12 + y = 18$, so $y = 6$. The solution is $x = 12$, $y = 6$.

17. Correct Answer: A (1)

The tangent of 45° is a standard trigonometric value: $\tan 45^\circ = 1$. This occurs in a 45-45-90 triangle where opposite and adjacent sides are equal, so their ratio equals 1. This is a value worth memorizing.

18. Correct Answer: D (9 cm)

If a rectangle has area 108 cm² and length 12 cm, use $A = l \times w$: $108 = 12 \times w$. Divide by 12: $w = 108/12 = 9$ cm. Verify: $12 \times 9 = 108 \checkmark$.

19. Correct Answer: C (36)

The least common multiple (LCM) of 12 and 18 can be found using prime factorization: $12 = 2^2 \times 3$, $18 = 2 \times 3^2$. The LCM uses the highest power of each prime: $LCM = 2^2 \times 3^2 = 4 \times 9 = 36$. Alternatively, list multiples: 12, 24, 36... and 18, 36... The first common multiple is 36.

20. Correct Answer: B (1/3)

With 4 red balls and 8 blue balls, there are 12 total balls. The probability of drawing a red ball is (number of red)/(total) = $4/12 = 1/3$. This tests basic probability calculation.

21. Correct Answer: D (5)

The distance formula is $d = \sqrt{[(x_2 - x_1)^2 + (y_2 - y_1)^2]}$. With points (3, 6) and (7, 9): $d = \sqrt{[(7-3)^2 + (9-6)^2]} = \sqrt{[4^2 + 3^2]} = \sqrt{[16 + 9]} = \sqrt{25} = 5$. This represents the 3-4-5 Pythagorean triple.

22. Correct Answer: A (40)

For direct variation, $y = kx$ where k is constant. When $y = 30$ and $x = 6$: $30 = k(6)$, so $k = 5$. When $x = 8$: $y = 5(8) = 40$. In direct variation, the ratio y/x remains constant.

23. Correct Answer: C (1/2)

The cosine of 60° is a standard trigonometric value: $\cos 60^\circ = 1/2$. This can be derived from a 30-60-90 triangle with sides in ratio $1:\sqrt{3}:2$, where $\cos 60^\circ = \text{adjacent/hypotenuse} = 1/2$. This is a value worth memorizing.

24. Correct Answer: B (144 cm²)

If a square has perimeter 48 cm, then $4s = 48$, so $s = 12$ cm (side length). The area is $A = s^2 = 12^2 = 144$ cm². This tests connecting perimeter and area formulas for squares.

25. Correct Answer: A (19)

Evaluate $f(x) = 6x - 11$ at $x = 5$ by substitution: $f(5) = 6(5) - 11 = 30 - 11 = 19$. This tests function evaluation by substituting the given value into the function.

26. Correct Answer: B (62.5%)

Convert $5/8$ to decimal first: $5 \div 8 = 0.625$. Then multiply by 100 to get percentage: $0.625 \times 100 = 62.5\%$. Alternatively, $5/8 = 625/1000 = 62.5\%$.

27. Correct Answer: D (8)

Solve $5x + 8 = 3x + 24$ by subtracting $3x$ from both sides: $2x + 8 = 24$. Subtract 8 from both sides: $2x = 16$. Divide by 2: $x = 8$. Verify: $5(8) + 8 = 40 + 8 = 48$, and $3(8) + 24 = 24 + 24 = 48$ ✓.

28. Correct Answer: A (240 cm³)

The volume of a rectangular prism is $V = \text{length} \times \text{width} \times \text{height}$. With dimensions $5 \text{ cm} \times 6 \text{ cm} \times 8 \text{ cm}$: $V = 5 \times 6 \times 8 = 240$ cm³. This is a direct application of the rectangular prism volume formula.

29. Correct Answer: C (14)

The greatest common factor (GCF) of 42 and 56 can be found using prime factorization: $42 = 2 \times 3 \times 7$ and $56 = 2^3 \times 7$. The GCF uses the lowest power of each common prime: $2 \times 7 = 14$.

30. Correct Answer: D (65°)

In any triangle, the three angles sum to 180° . With angles 50° , 65° , and x° : $50 + 65 + x = 180$, so $115 + x = 180$, giving $x = 65^\circ$. This tests the fundamental triangle angle sum property.

31. Correct Answer: D (52)

Calculate $6^2 + 4^2$: First, $6^2 = 36$. Then, $4^2 = 16$. Finally, $36 + 16 = 52$. This tests exponent evaluation and addition.

32. Correct Answer: C (5/8)

To subtract fractions with different denominators, find a common denominator. The LCD of 4 and 8 is 8: $3/4 = 6/8$. Then $6/8 - 1/8 = 5/8$. This tests fraction subtraction with unlike denominators.

33. Correct Answer: B (452.16 cm³)

The volume of a cylinder is $V = \pi r^2 h$. With $r = 4$ cm, $h = 9$ cm, and $\pi \approx 3.14$: $V = 3.14 \times 4^2 \times 9 = 3.14 \times 16 \times 9 = 3.14 \times 144 = 452.16$ cm³. This tests applying the cylinder volume formula.

34. Correct Answer: D (49)

To increase 35 by 40%, calculate 40% of 35 and add: $0.40 \times 35 = 14$, so $35 + 14 = 49$. Alternatively, 35 increased by 40% = $35 \times 1.40 = 49$.

35. Correct Answer: A (60°)

If $\tan \theta = \sqrt{3}$, then $\theta = 60^\circ$ (in the range $0^\circ < \theta < 90^\circ$). This occurs in a 30-60-90 triangle where the opposite and adjacent sides are in the ratio $\sqrt{3}:1$, so $\tan 60^\circ = \sqrt{3}$. This is a standard trigonometric value worth memorizing.

36. Correct Answer: C (19)

Solve $3(x - 4) = 2x + 7$ by first distributing: $3x - 12 = 2x + 7$. Subtract $2x$ from both sides: $x - 12 = 7$. Add 12 to both sides: $x = 19$. Verify: $3(19 - 4) = 3(15) = 45$, and $2(19) + 7 = 38 + 7 = 45$ ✓.

37. Correct Answer: B (20)

Range equals maximum minus minimum. In the dataset $\{15, 28, 20, 35, 22\}$, the maximum is 35 and minimum is 15. Range = $35 - 15 = 20$. This tests understanding of range as a measure of spread.

38. Correct Answer: D (± 12)

If $x^2 = 144$, then $x = \pm\sqrt{144} = \pm 12$. Both positive and negative 12 are solutions because $(12)^2 = 144$ and $(-12)^2 = 144$. Always consider both positive and negative square roots when solving $x^2 = \text{constant}$.

39. Correct Answer: A (1/2)

The sine of 30° is a standard trigonometric value: $\sin 30^\circ = 1/2$. This can be derived from a 30-60-90 triangle with sides in ratio $1:\sqrt{3}:2$, where $\sin 30^\circ = \text{opposite/hypotenuse} = 1/2$. This is a value worth memorizing.

40. Correct Answer: C ($4x^2y^2$)

Simplify $(12x^5y^4)/(3x^3y^2)$ by dividing coefficients and subtracting exponents for like bases. For the coefficient: $12/3 = 4$. For x : $x^5/x^3 = x^{(5-3)} = x^2$. For y : $y^4/y^2 = y^{(4-2)} = y^2$. The result is $4x^2y^2$.